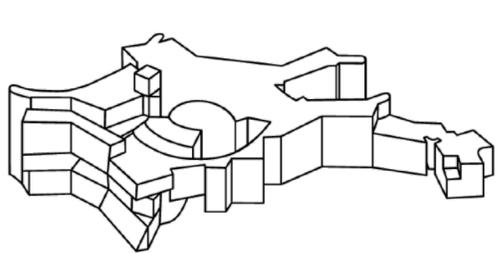


# REMOVAL AND MARGINALIZATION OF WELL-KNOWN CMB INSTRUMENTAL SYSTEMATICS

**Adri Duivenvoorden**

**Max Planck Institute for Astrophysics**



**MAX-PLANCK-INSTITUT  
FÜR ASTROPHYSIK**

**CosmoForward meeting  
09-02-2026**

# CMB INSTRUMENTAL SYSTEMATICS

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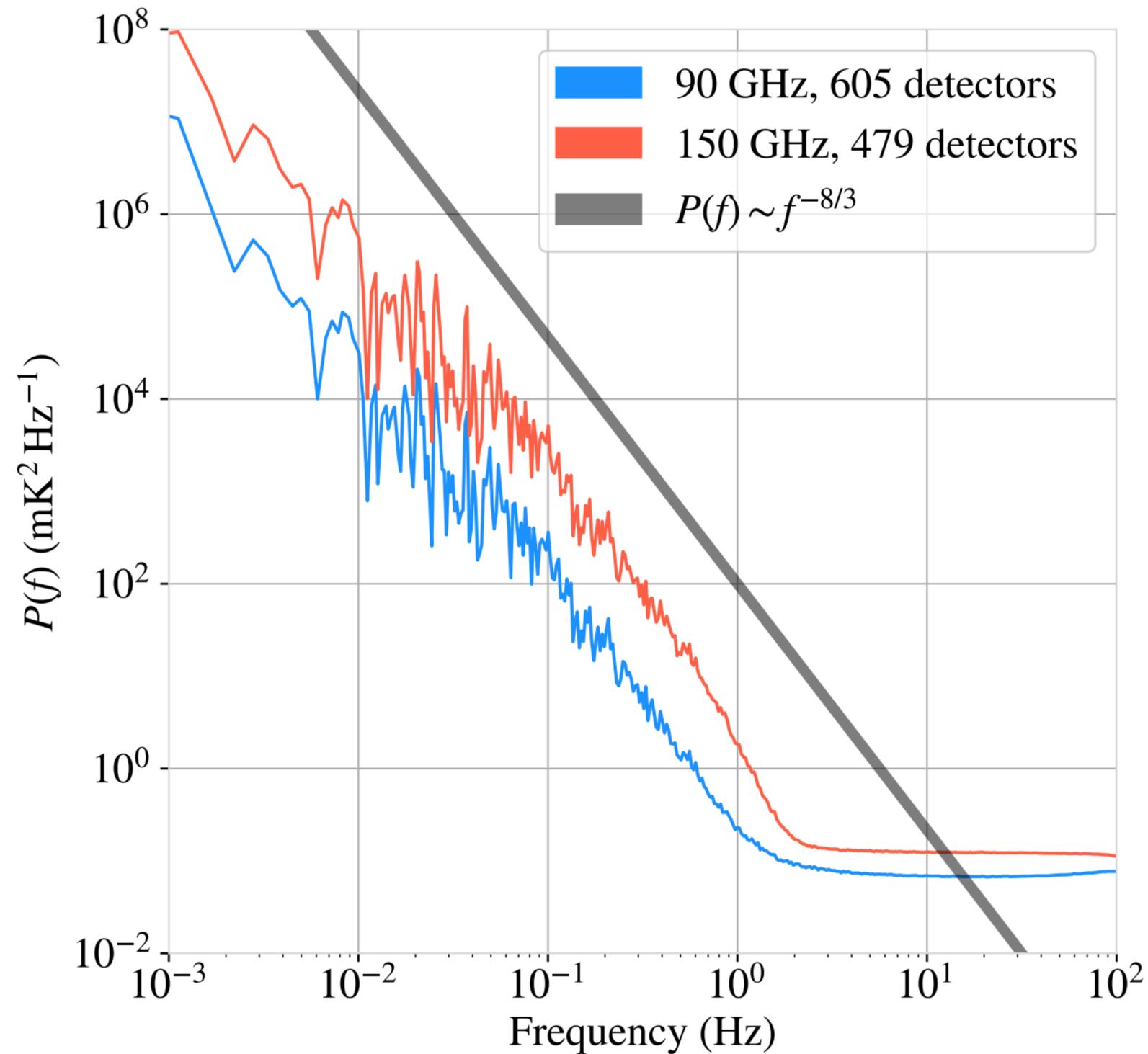
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  - ▶ Although the topics will be skewed towards my own experience with the Atacama Cosmology Telescope

# ATMOSPHERIC NOISE

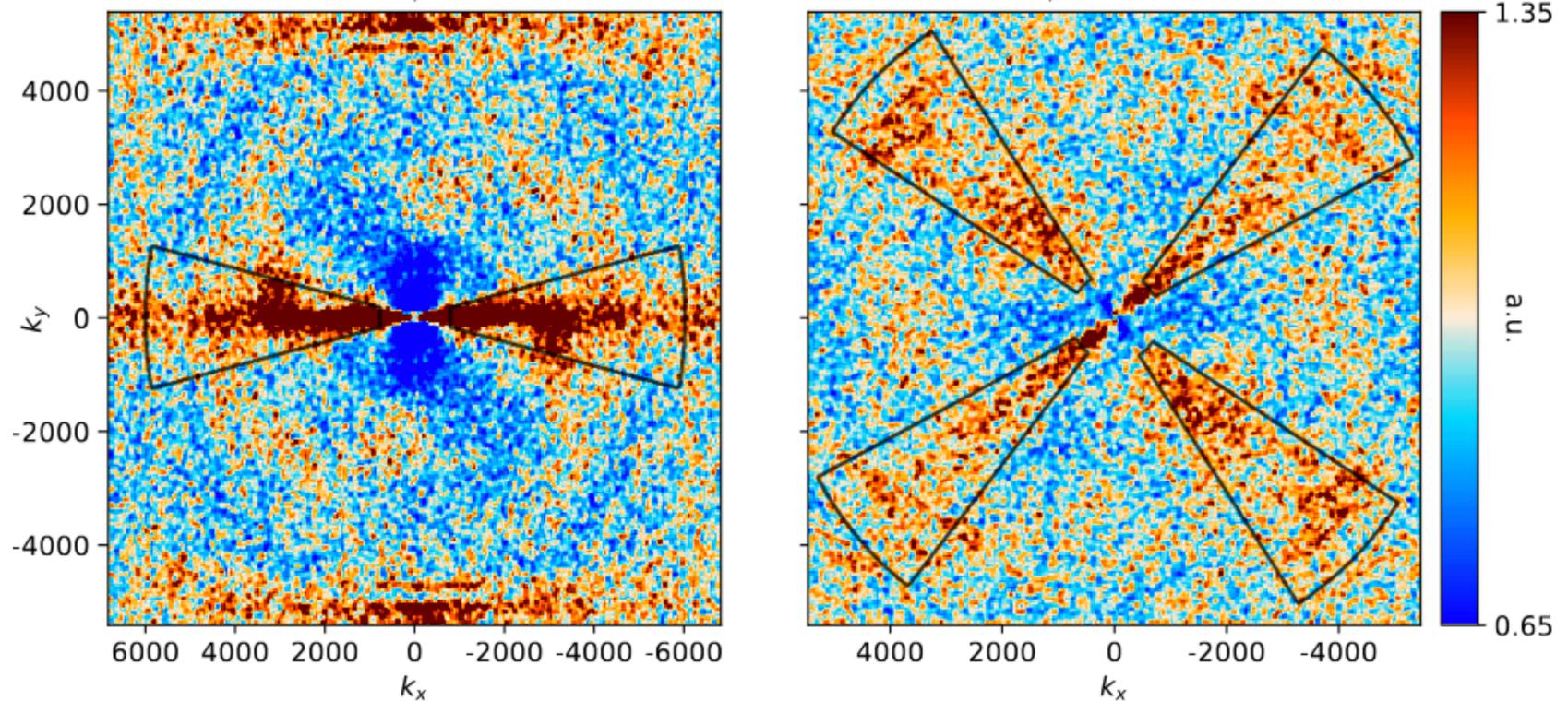


33 minutes of stare data  
for PA6

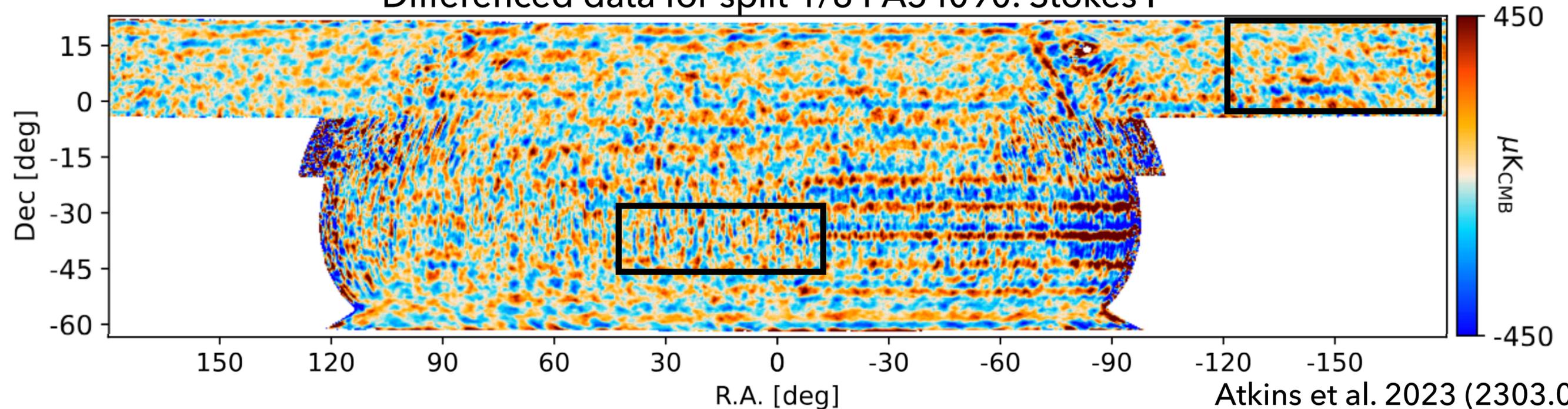
# NOISE PROPERTIES

Correlated atmospheric noise modulated by scan strategy results in complicated noise properties

- ▶ Difficult to simulate the atmosphere



Differenced data for split 1/8 PA5 f090. Stokes I

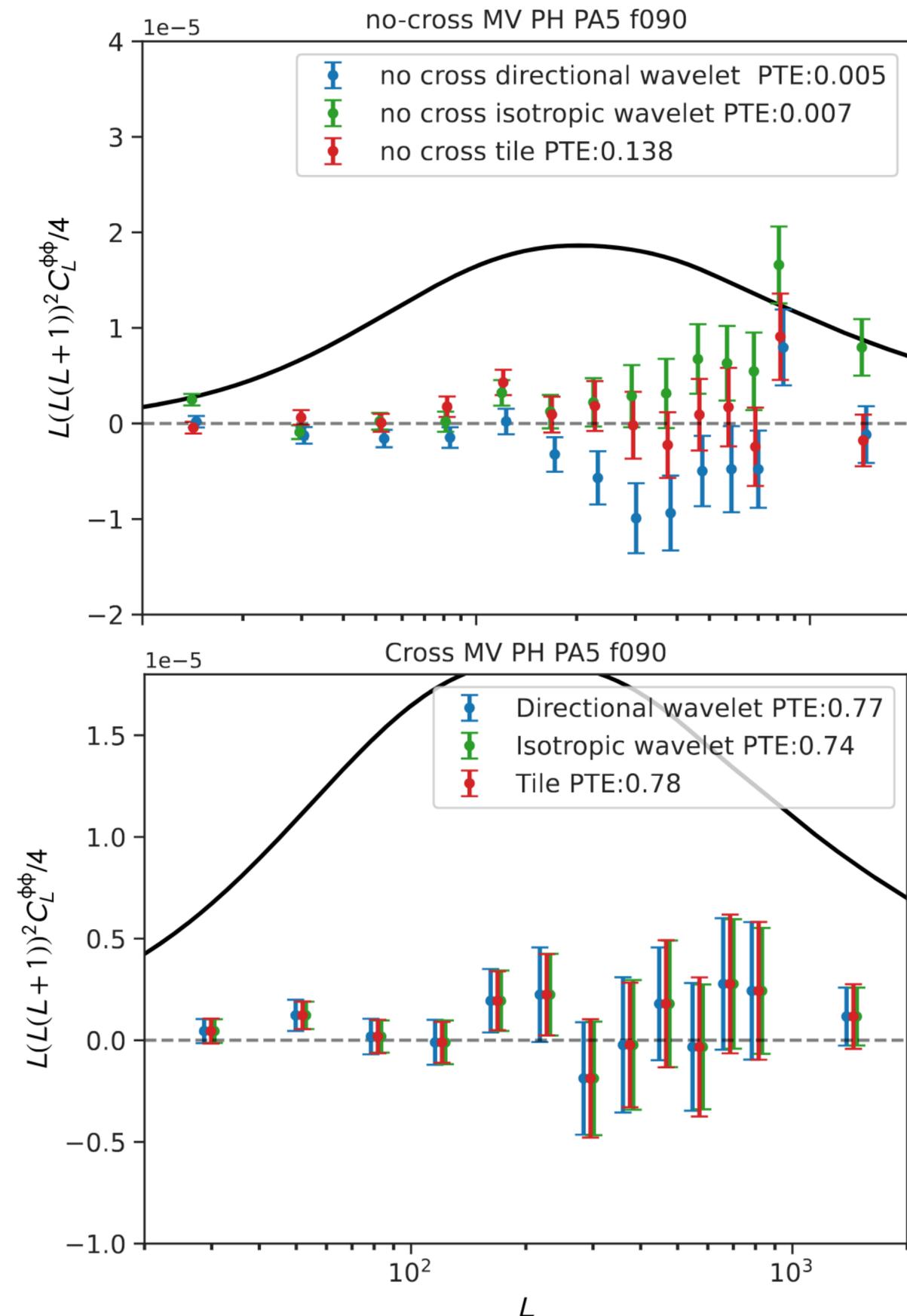


Atkins et al. 2023 (2303.04180)

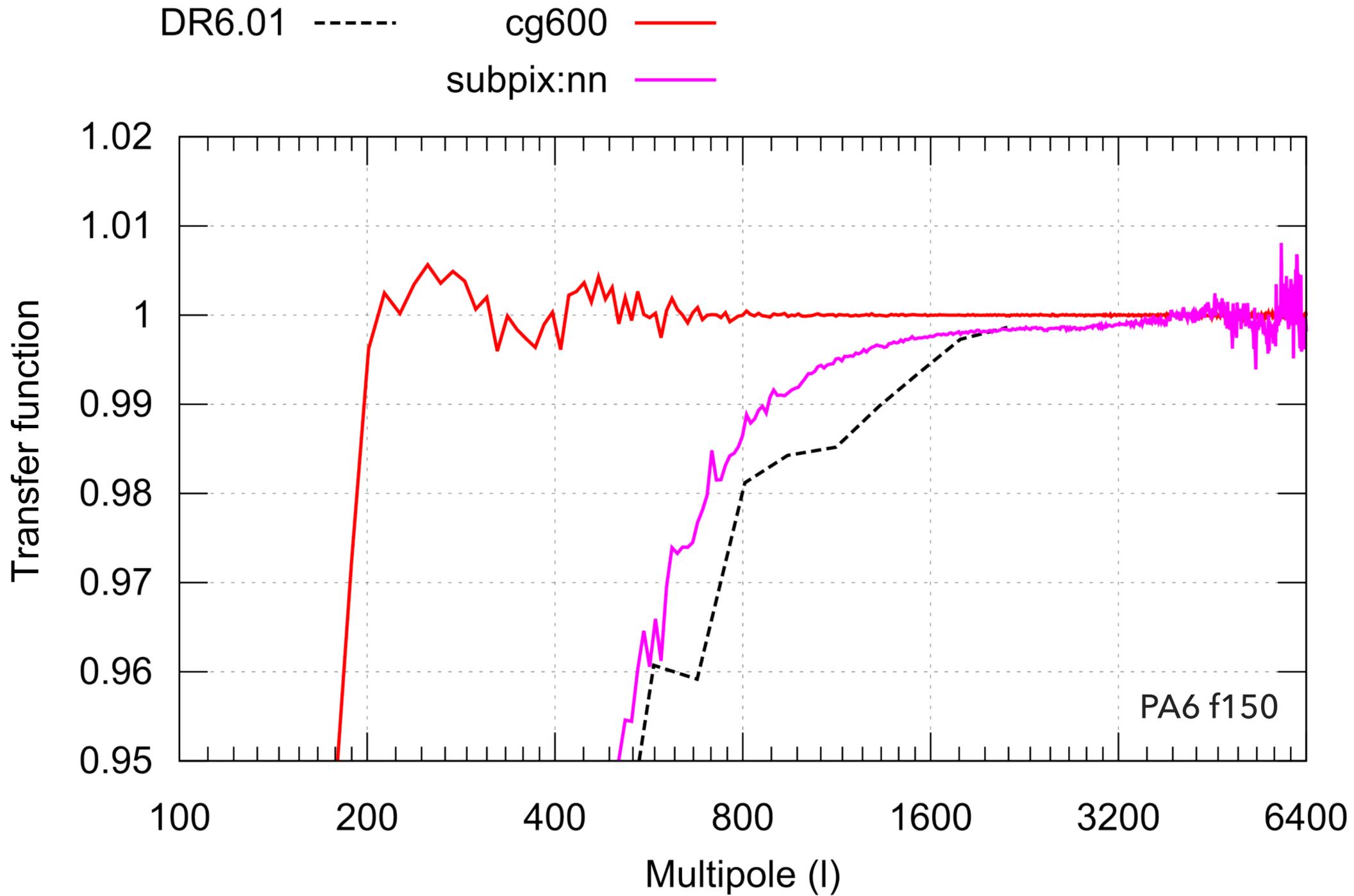
# ROBUST ESTIMATORS

Construct estimators that rely on the cross-correlation between observations with independent noise

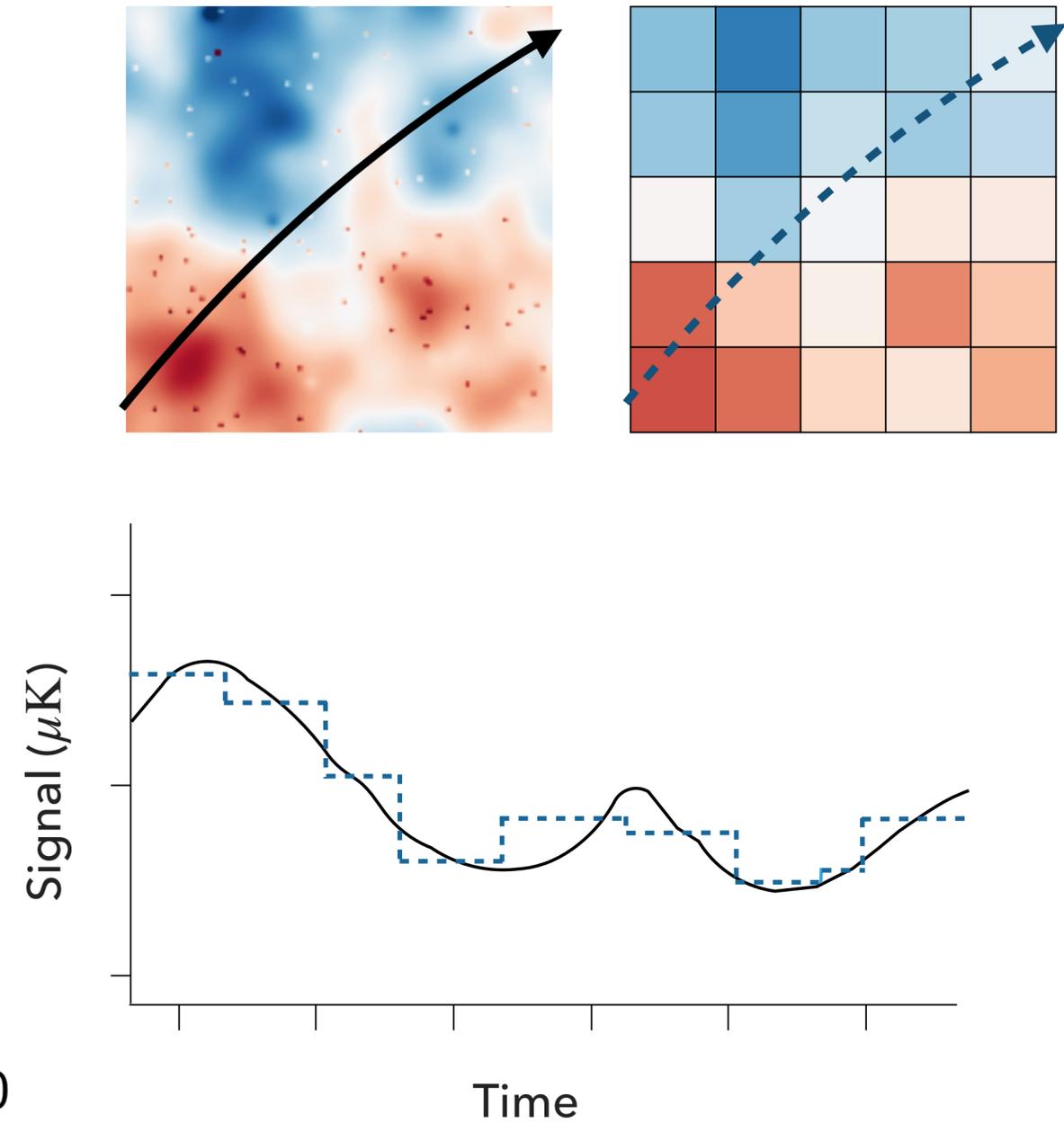
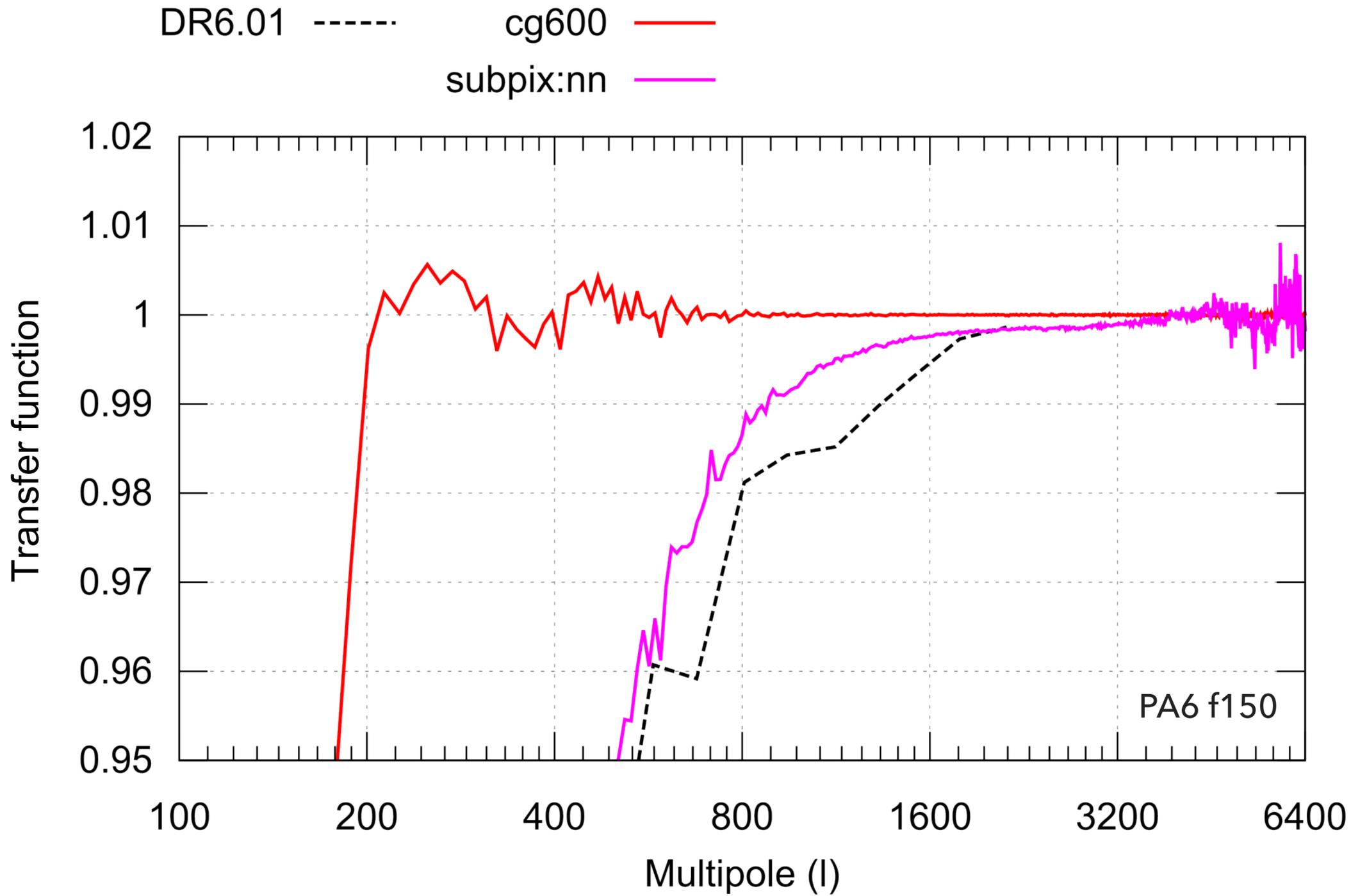
- ▶ Already the norm for power-spectrum estimation
- ▶ ACT DR6 demonstrated the effectiveness of this same idea for lensing estimation, using the estimator from Madhavacheril et al. (2020), 2011.02475



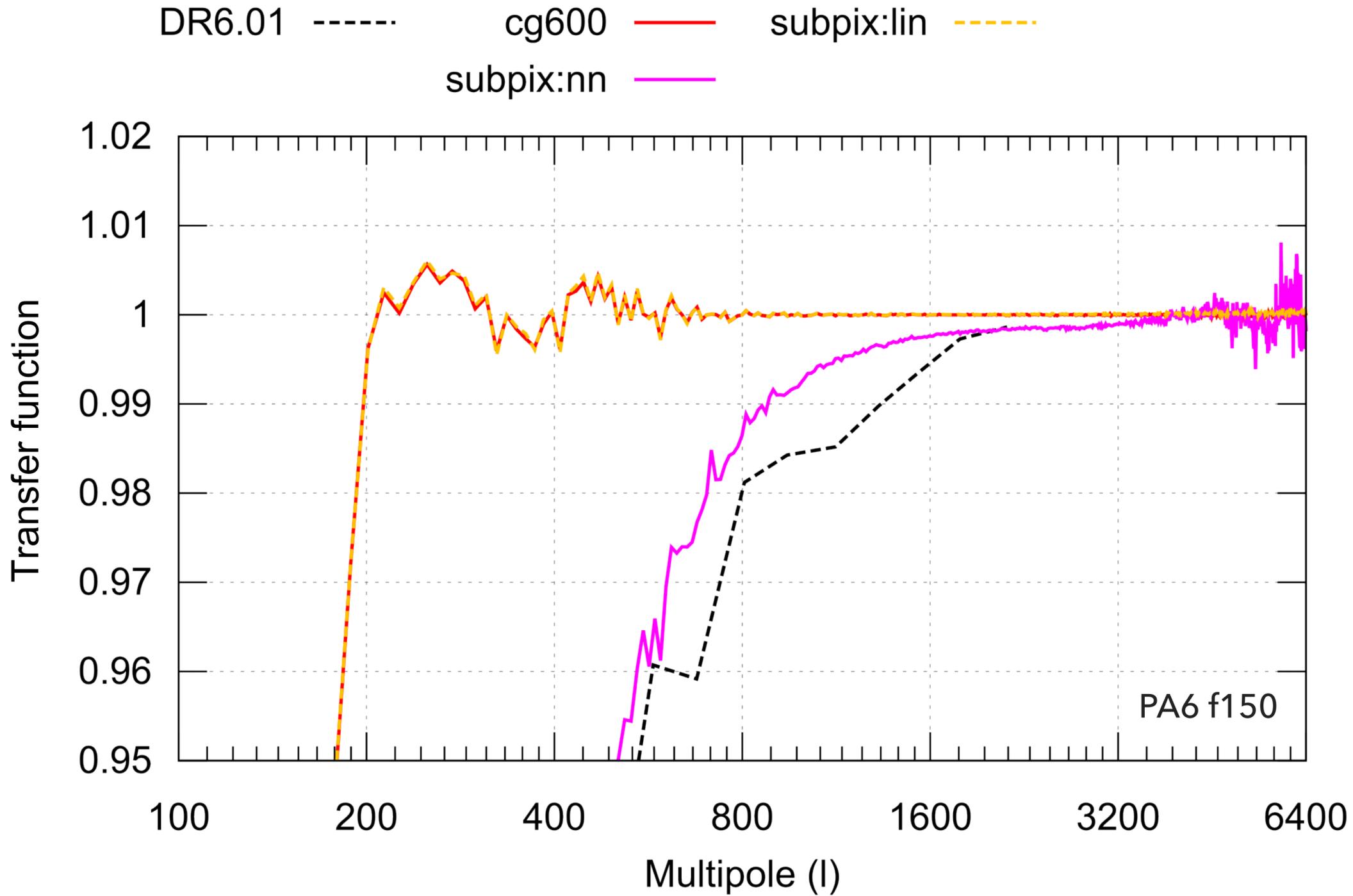
# MAPMAKING SYSTEMATICS

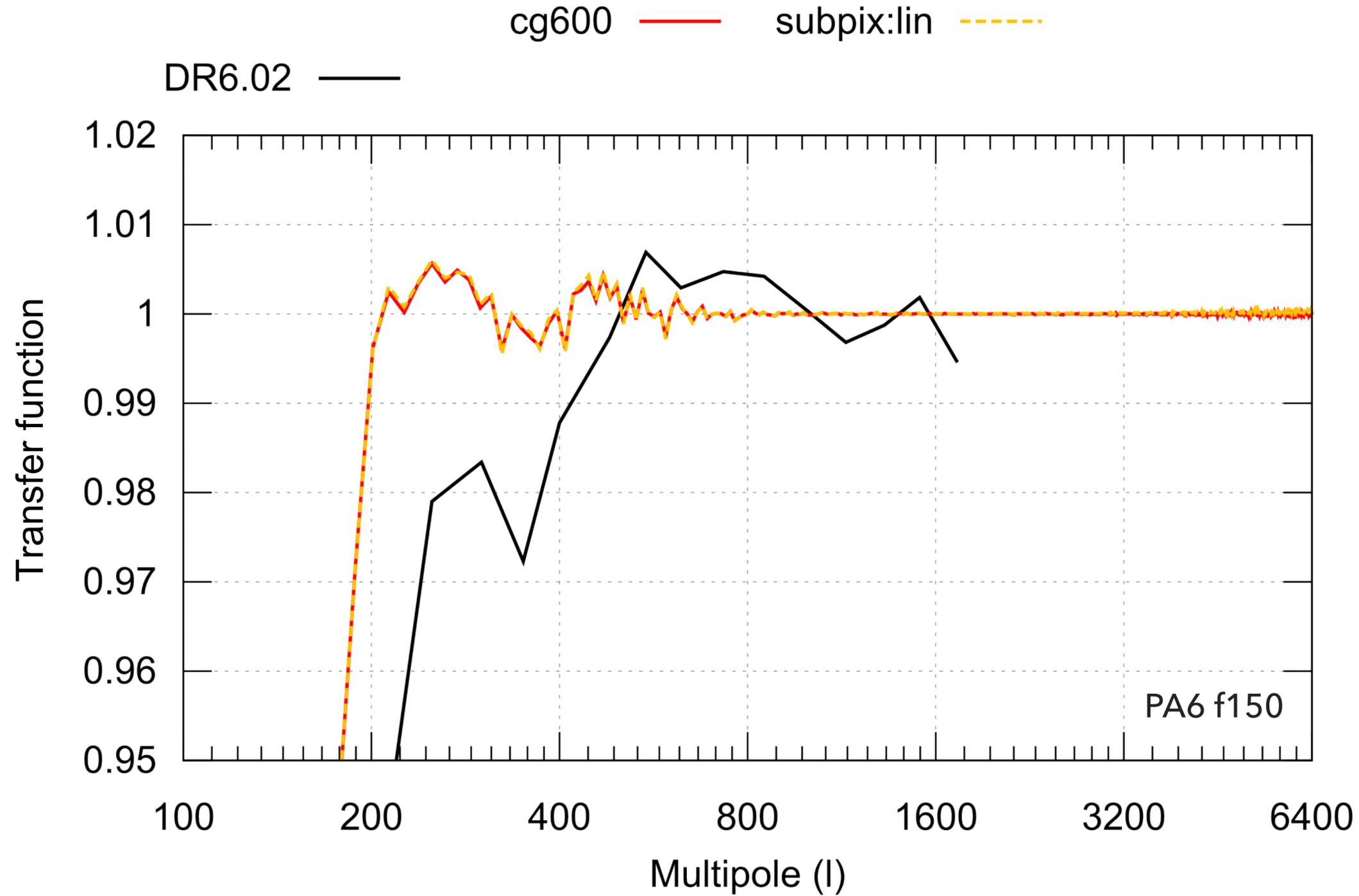


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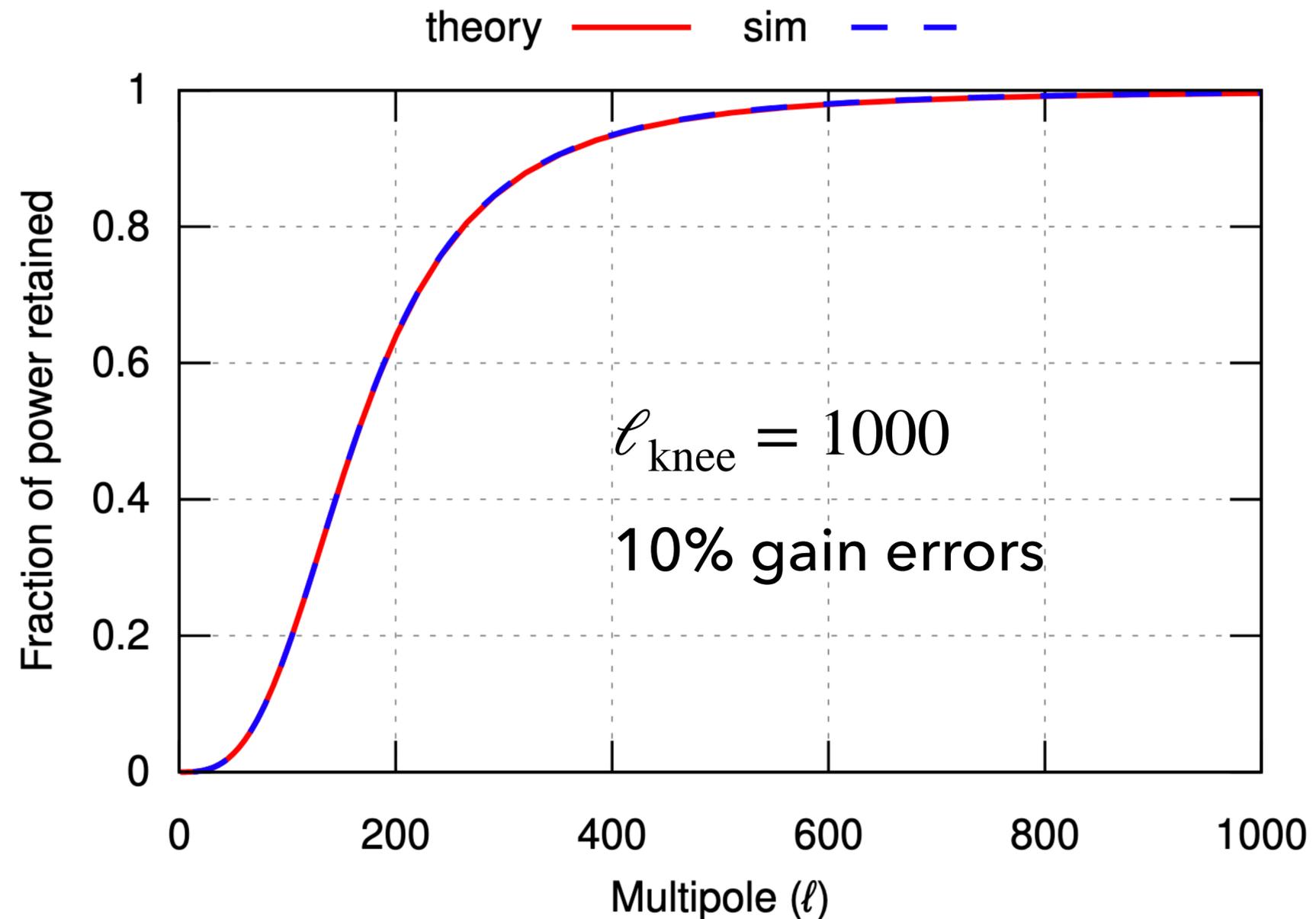
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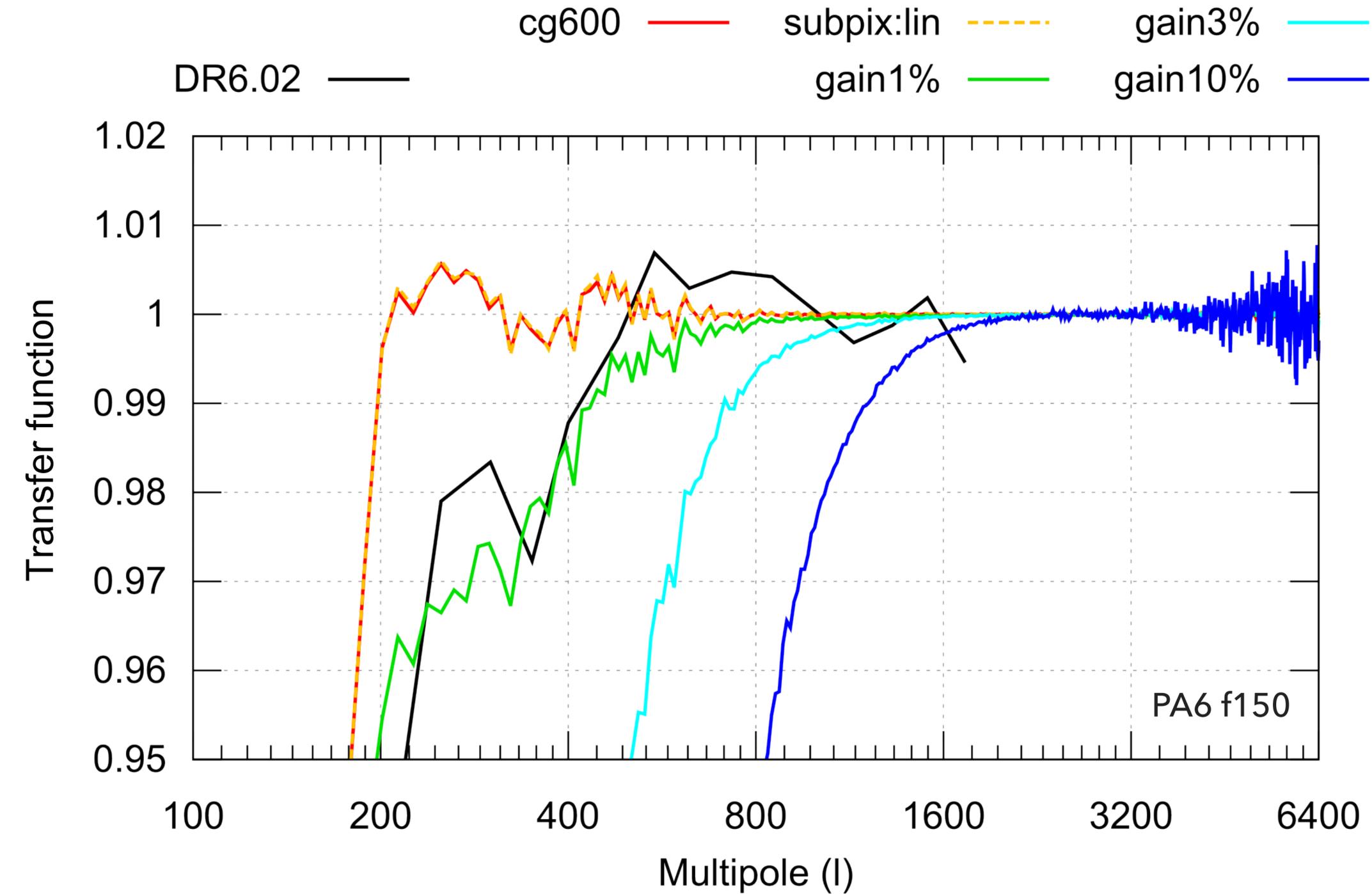
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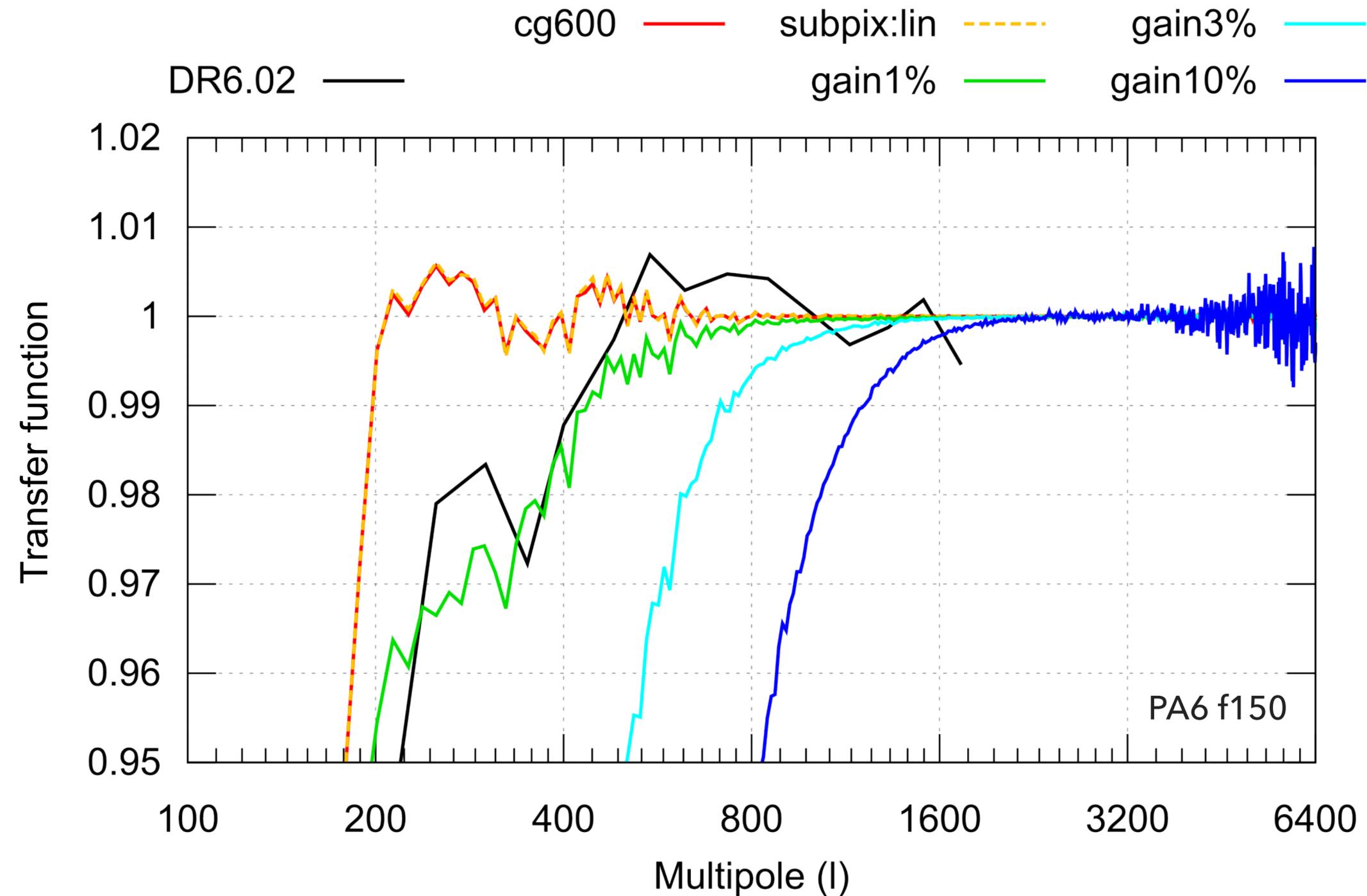
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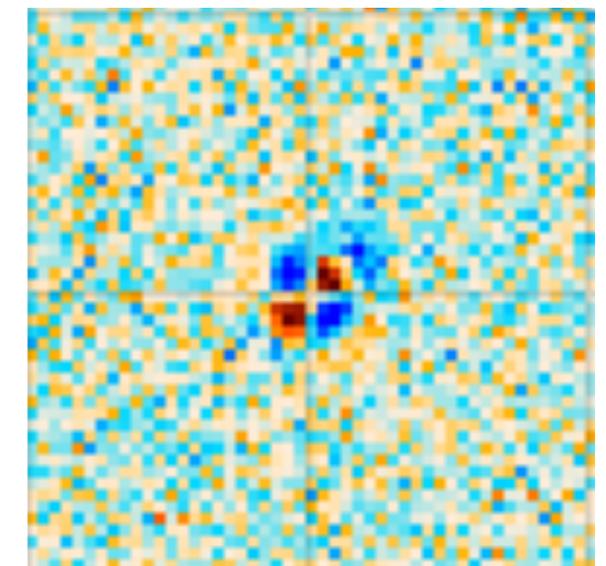
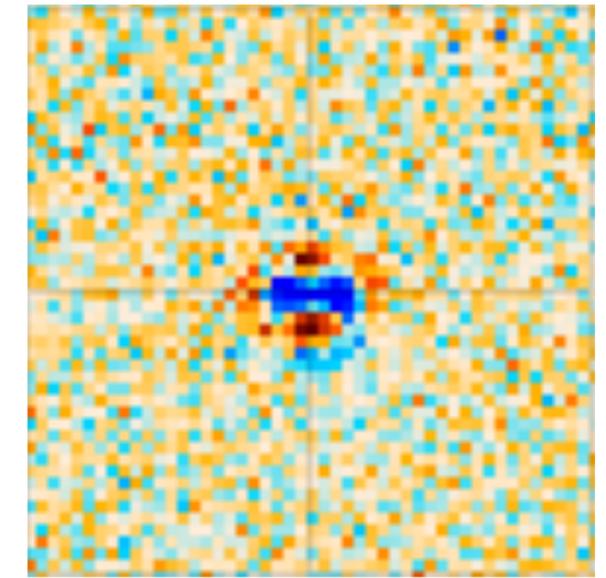
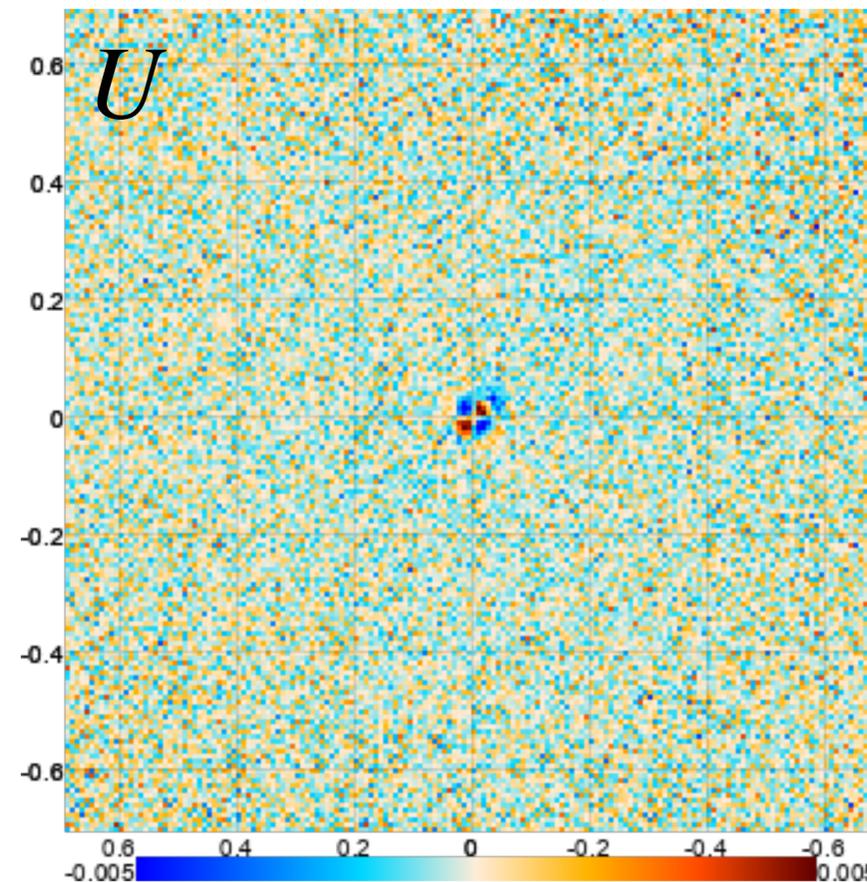
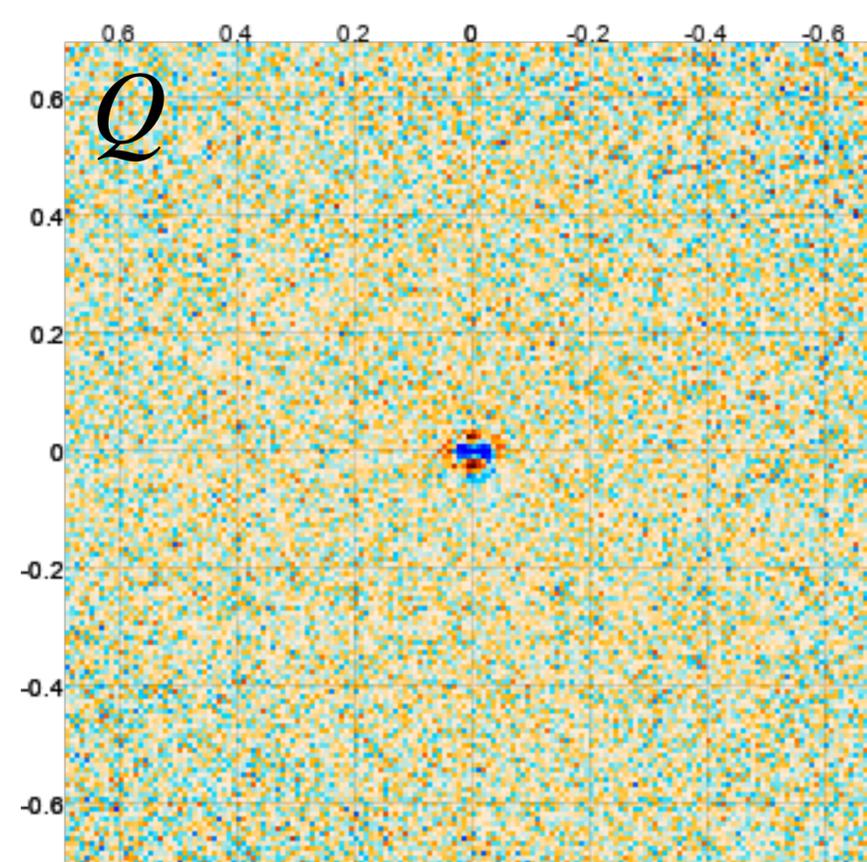
Final ACT DR6 transfer function consistent with  $\sim 1\%$  relative gain errors between detectors

- ▶ Difficult to improve much with either planet- or atmospheric-based calibration
- ▶ Improvements will likely require dedicated calibration hardware

# TEMPERATURE-TO-POLARIZATION LEAKAGE

Optical non-idealities and errors in the data model cause spurious polarized signal

- ▶ Quantified using planet observations

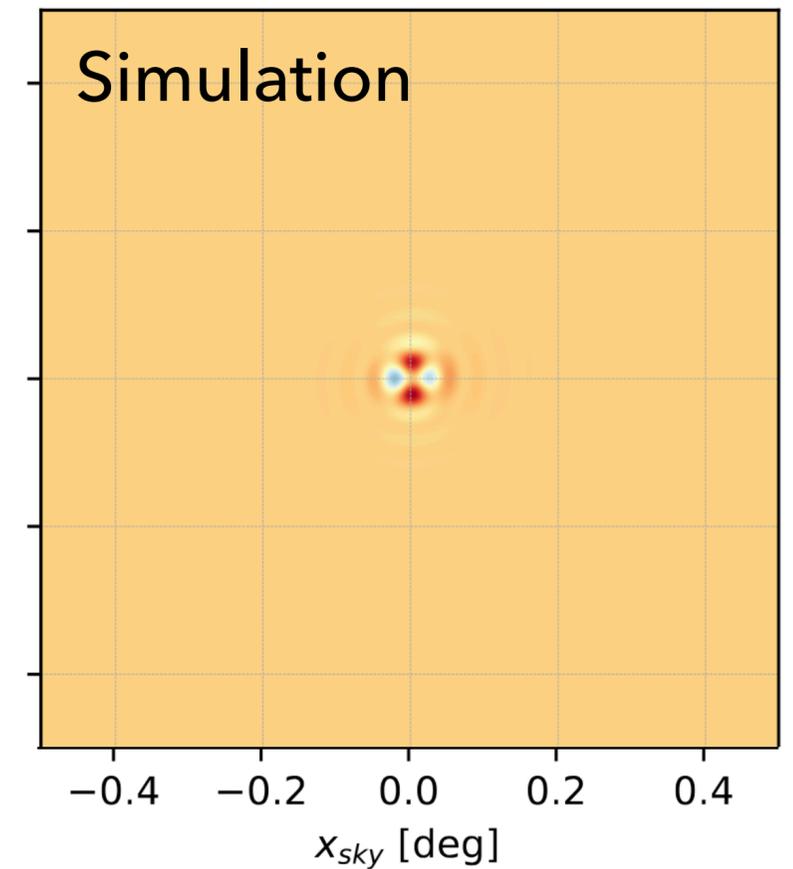
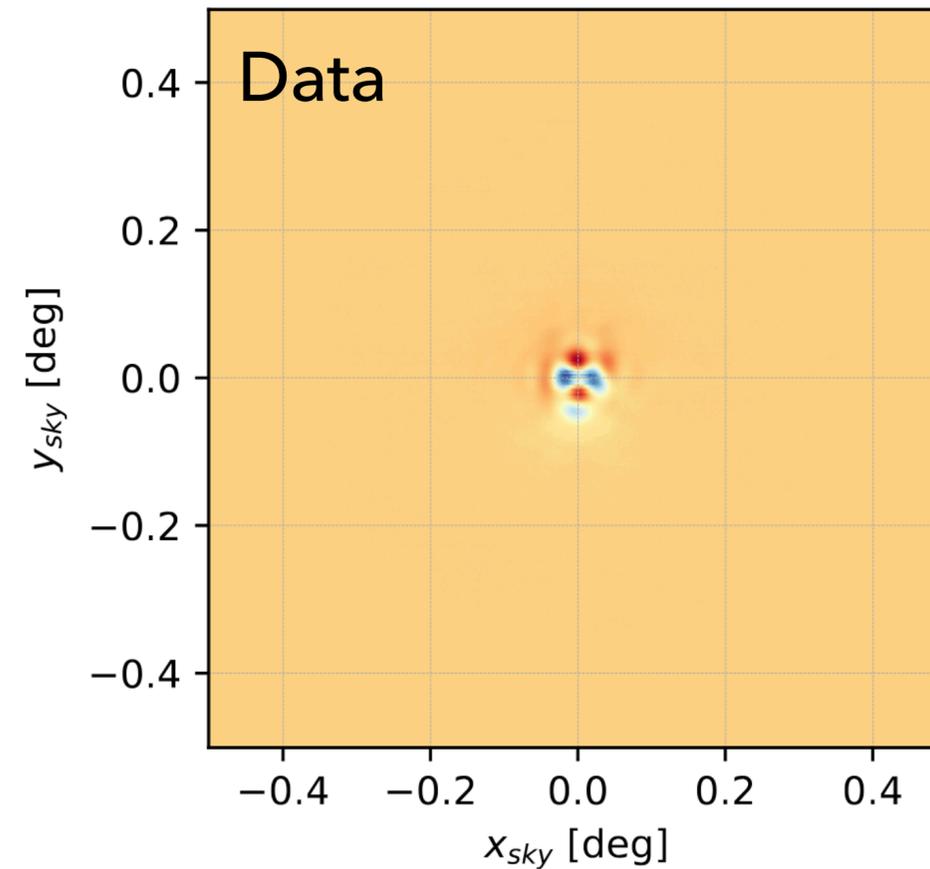


0.7x0.7 deg<sup>2</sup> maps of 25 Uranus observations

# OPTICAL SIMULATIONS ARE DIFFICULT

Simulations reveal that the bulk of the leakage at small scales is caused by geometry of the optics

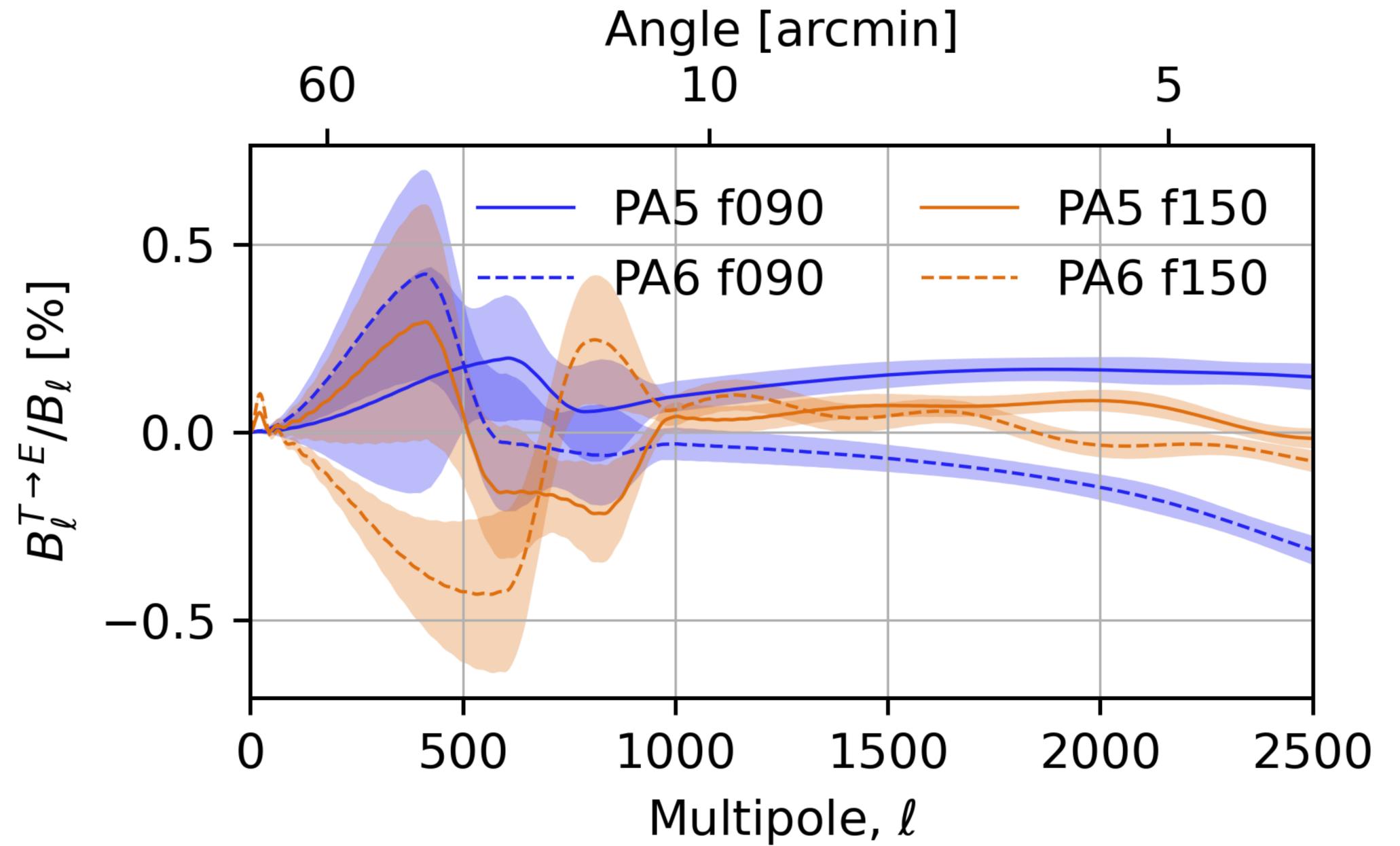
- ▶ Leakage at large angular scales appears to be caused by unknown mis-modeling (e.g. gain errors)



- ▶ Simulation by Roberto Puddu

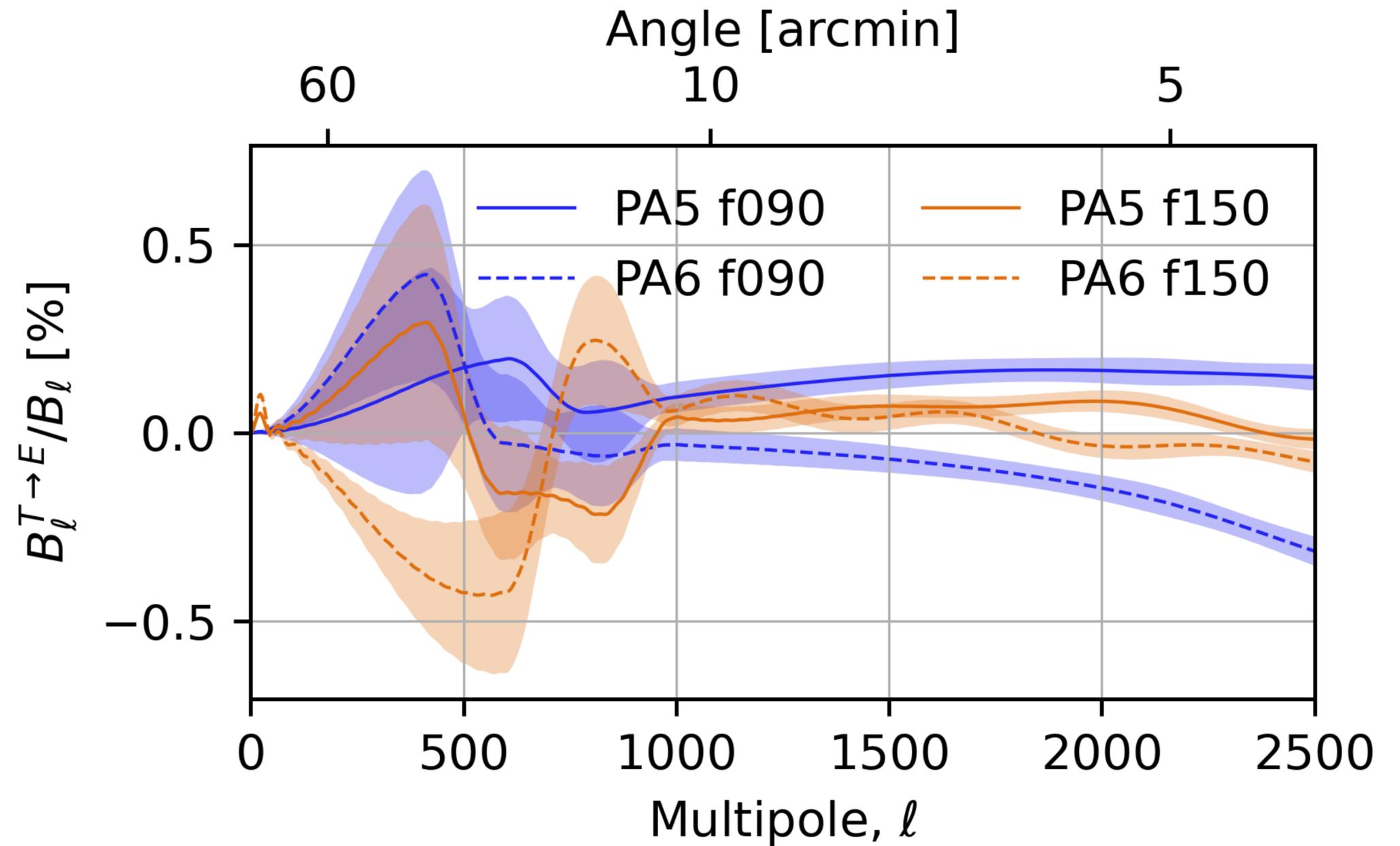
GRASP simulation of single detector on the center of the focal plane

No gain errors simulated, just the mirrors and lenses



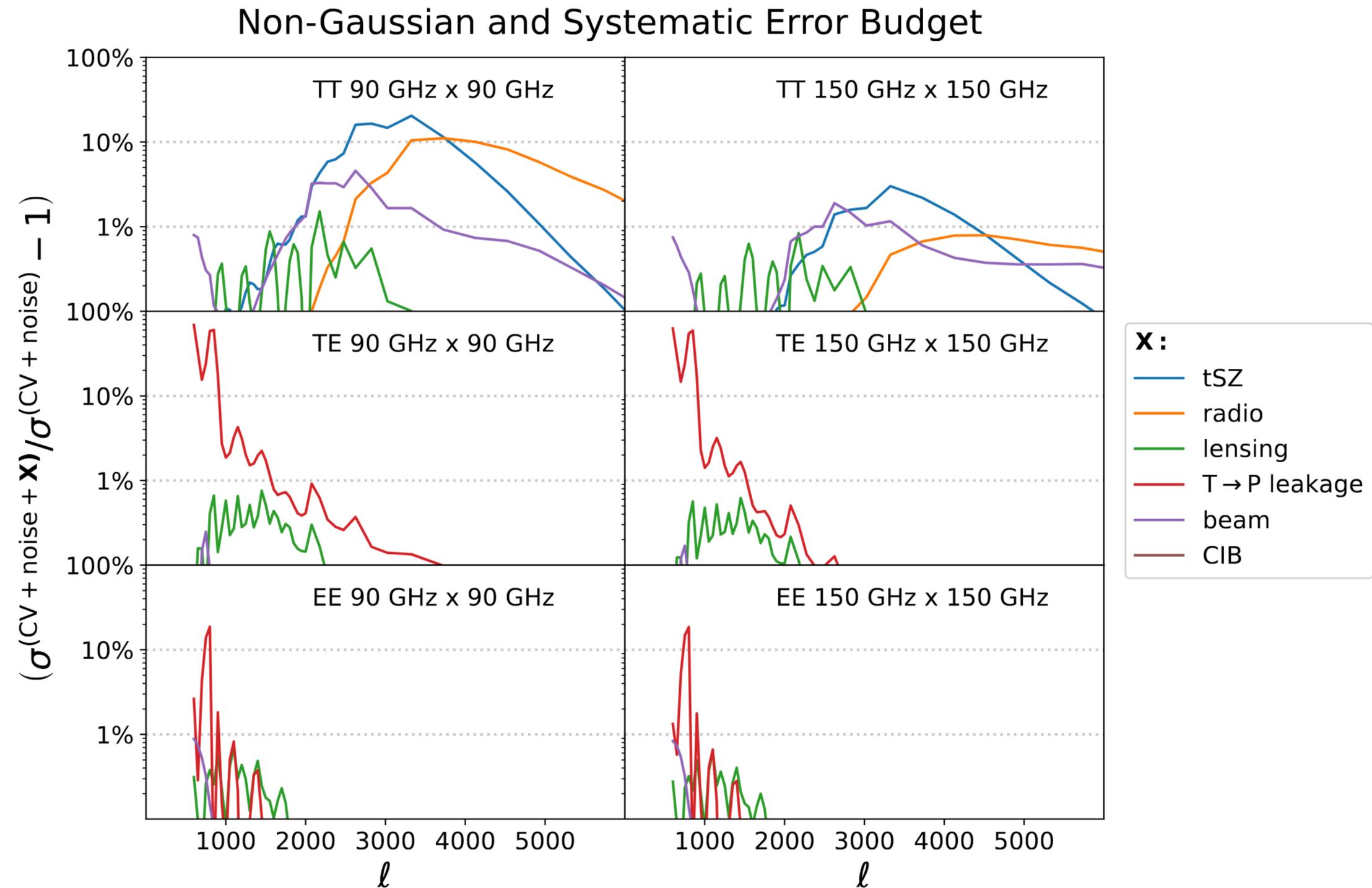
# BEAM LEAKAGE MODEL

Difficult to get good SNR measurements of the leakage at large angular scales



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- ▶ Leakage error dominates error budget at large scales



# POLARIZED BEAM

$$\begin{pmatrix} B^{II} & B^{IQ} & B^{IU} & B^{IV} \\ B^{QI} & B^{QQ} & B^{QU} & B^{QV} \\ B^{UI} & B^{UQ} & B^{UU} & B^{UV} \\ B^{VI} & B^{VQ} & B^{VU} & B^{VV} \end{pmatrix}$$

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- ▶ How do we directly measure our coupling to the polarized sky?
  - ▶ Polarized astrophysical sources

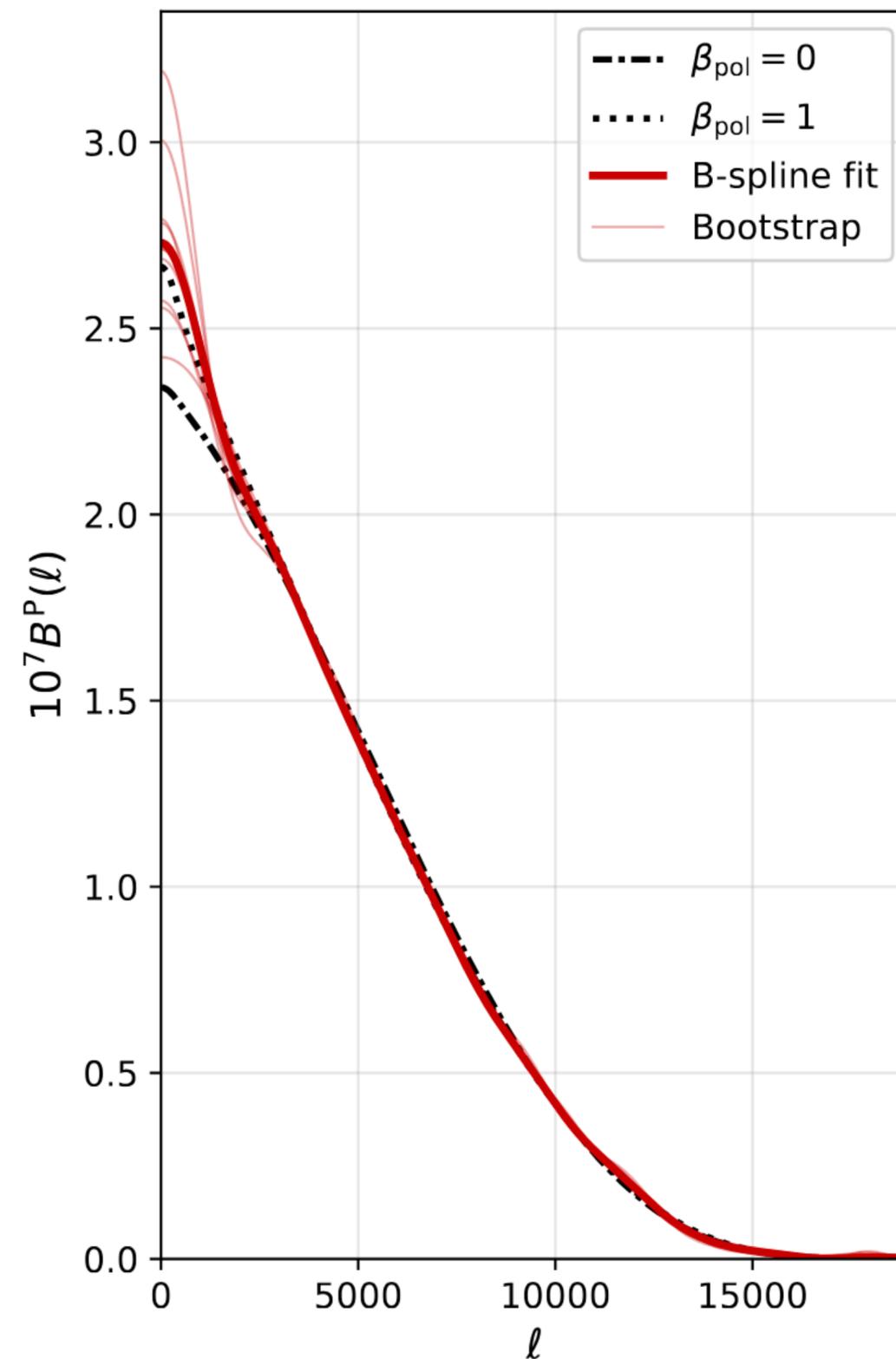
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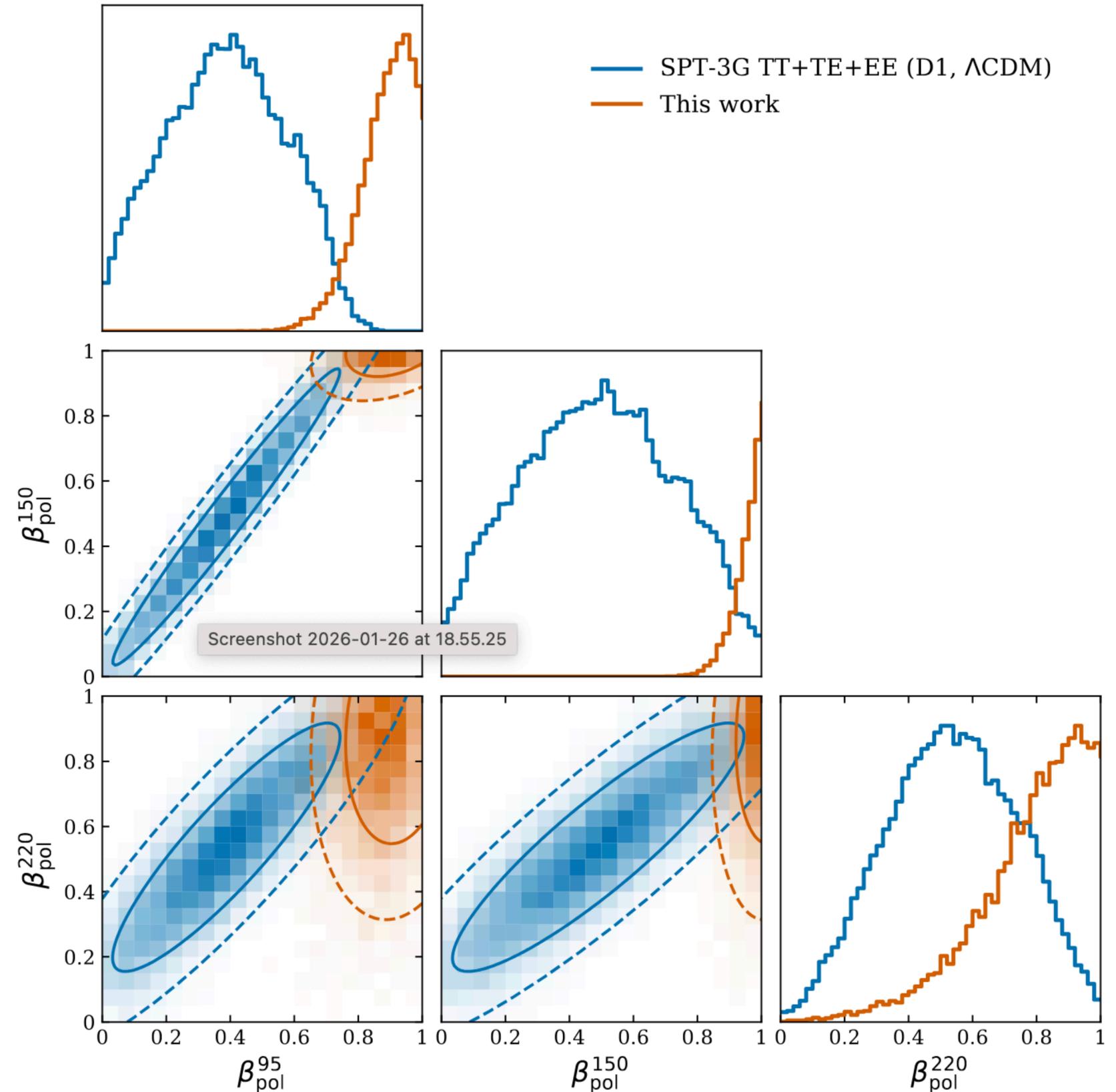
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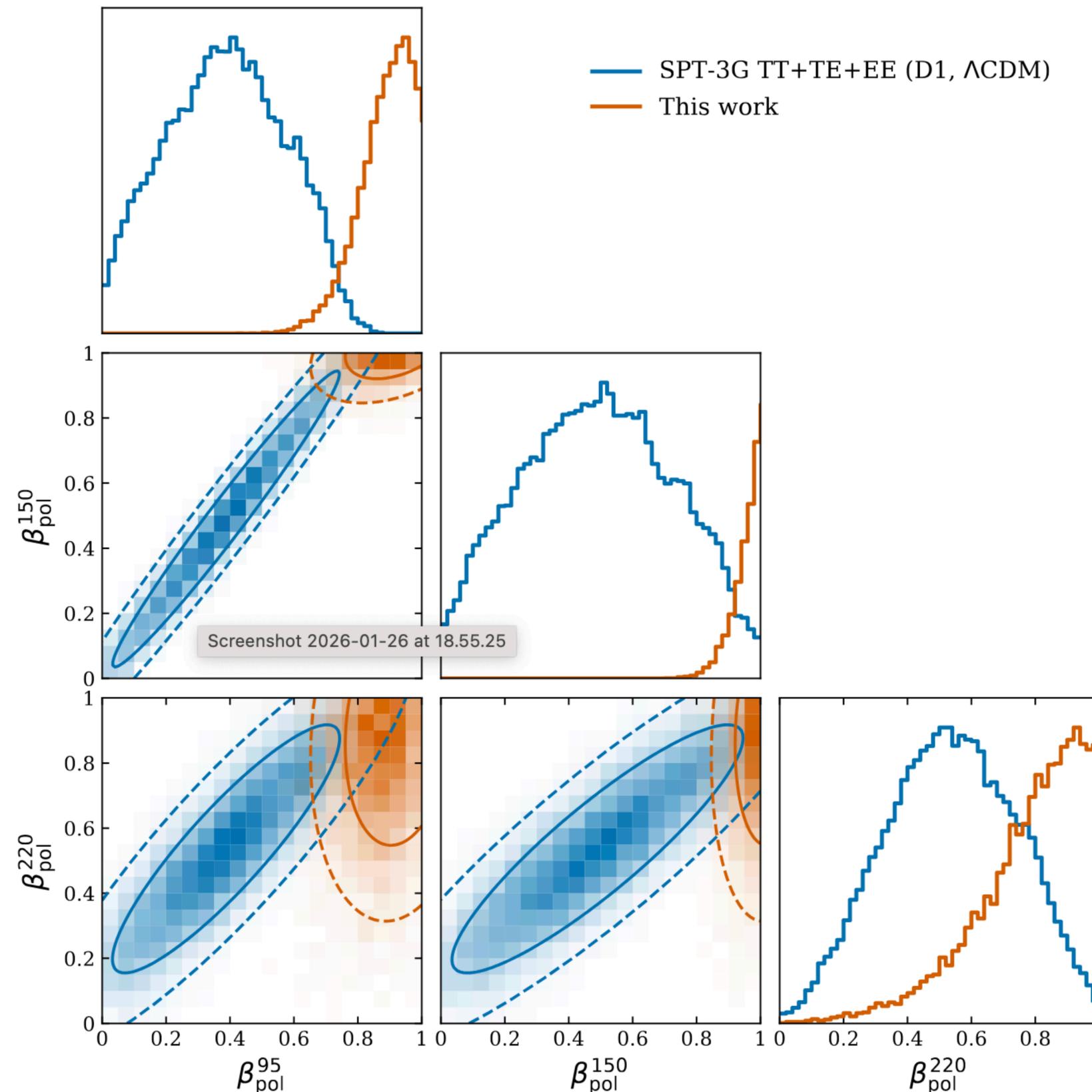
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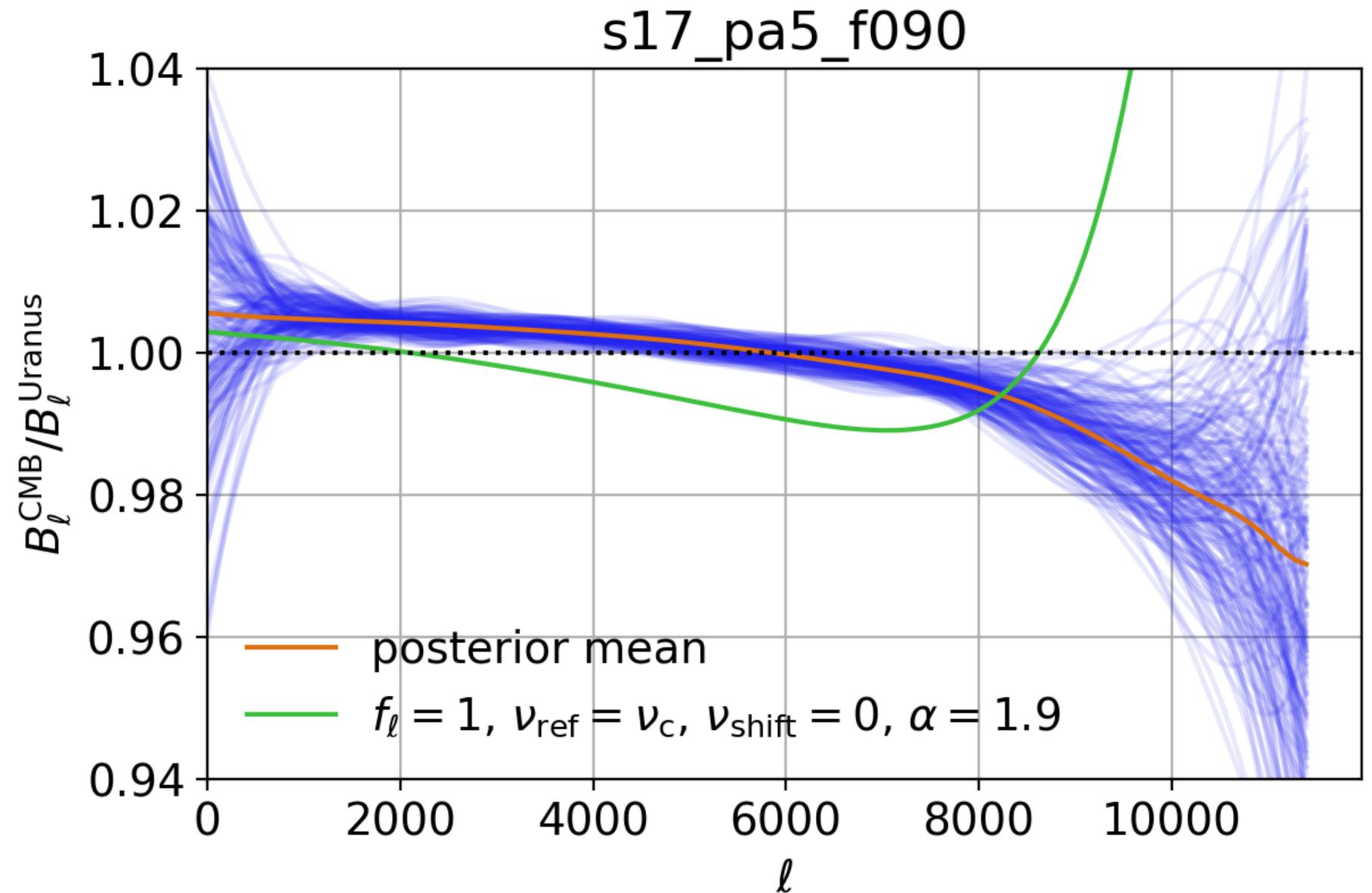
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- ▶ How do we directly measure our coupling to the polarized sky?
- ▶ Polarized astrophysical sources
- ▶ "Repurpose" calibration sources designed for polarization angle calibration, e.g. drone calibration



Frequency-dependence of the beam slightly changes beam shape for each sky component

$$\blacktriangleright B_{\ell}^c = \int B_{\ell}(\nu) I^c(\nu) \tau(\nu) d\nu$$



- ▶ Example of color-corrected beam for the CMB sky component

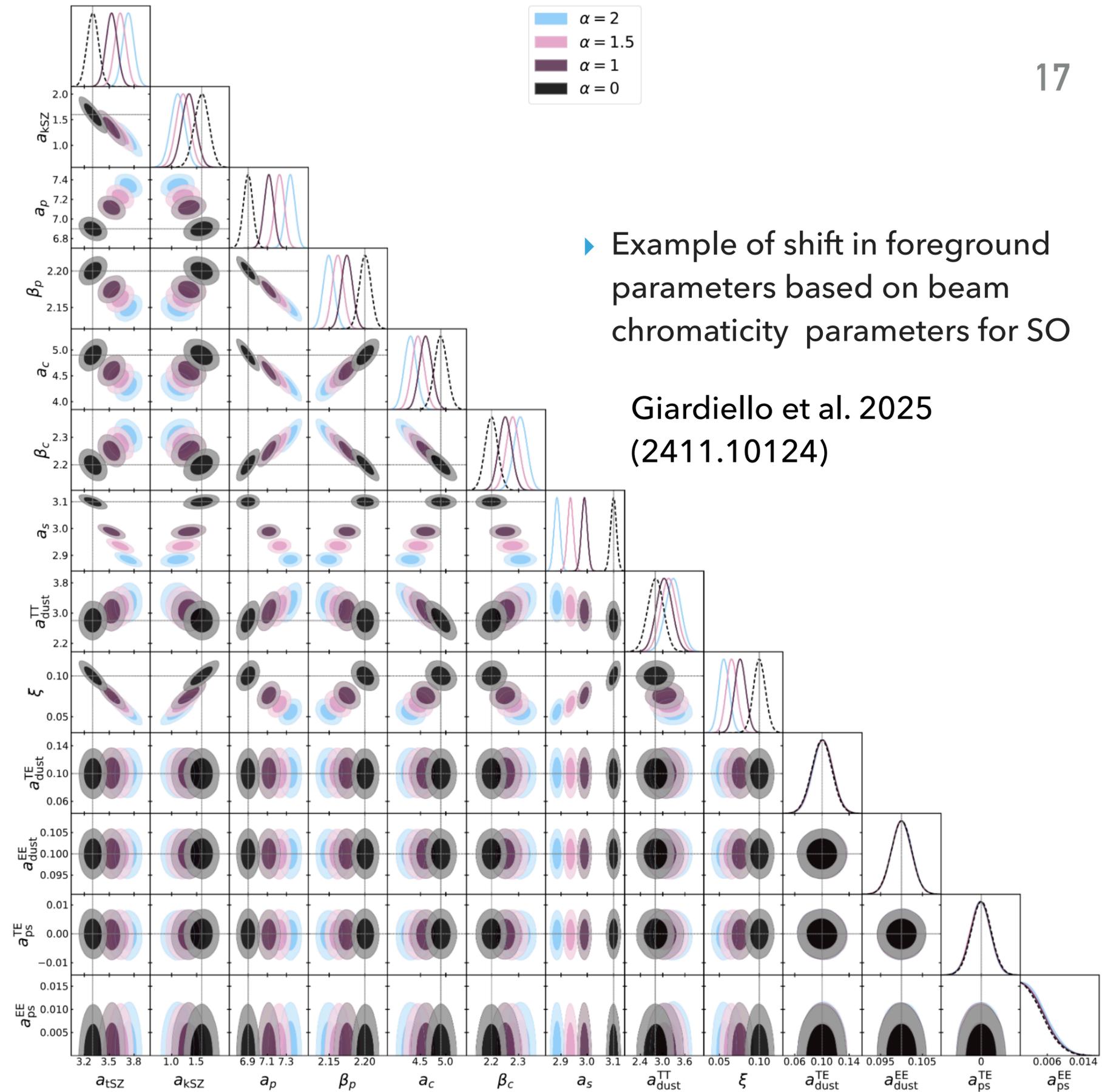
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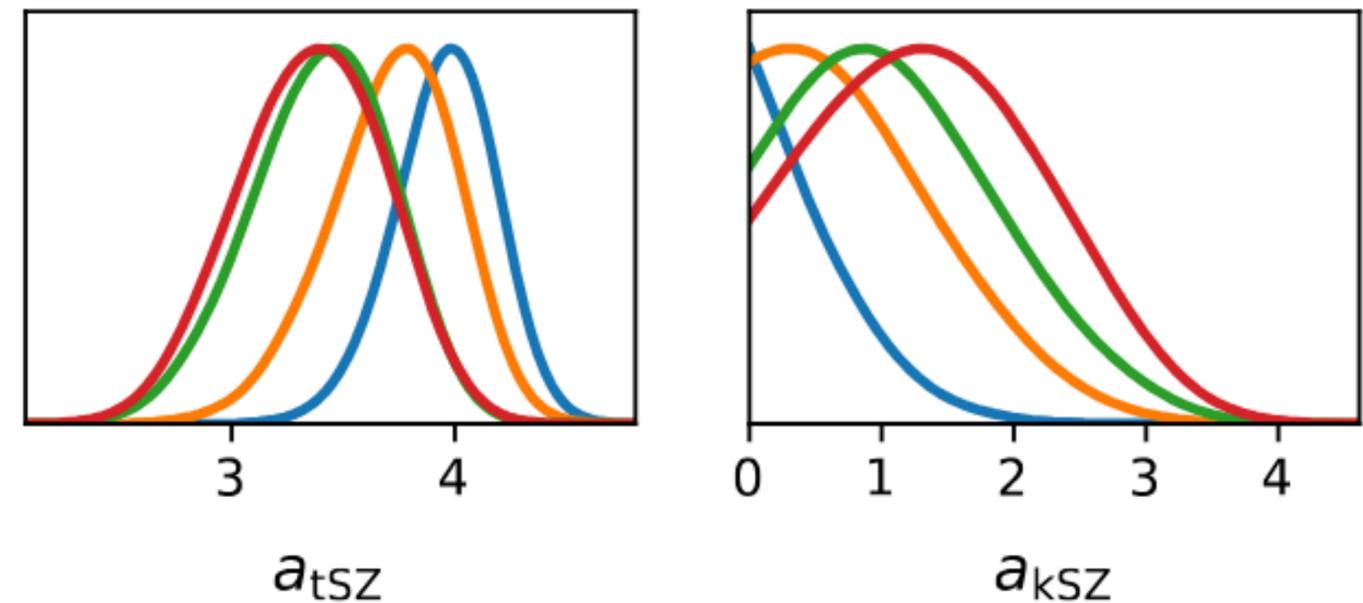
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Unblinding

+  $\alpha_{\text{tSZ}}$  marginalization

+  $\alpha_{\text{tSZ}}$  + beam chromaticity

Baseline ( $\alpha_{\text{tSZ}}$  + chromatic beams + polarization cuts)



▶ ACT DR6 shifts in foreground parameters due to beam chromaticity

# MARGINALIZATION OVER NUISANCE PARAMETERS

$$\blacktriangleright P(\vec{\theta} | \vec{d}) = \int P(\vec{\theta}, \vec{\phi} | \vec{d}) d\vec{\phi}$$

- ▶  $\vec{\theta}$ : Cosmological parameters, e.g.  $r$
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- ▶ Option 2: directly target  $P(\vec{\theta} | \vec{d})$  using simulation-based inference
  - ▶ Well-suited for systematics-dominated analyses, like CMB searches for  $r$
  - ▶ NB. really target  $P(\vec{\theta} | \vec{x})$ , where  $\vec{x} = f(\vec{d})$  is a compressed representation of the data that suppresses part of its complexity

# NEURAL POSTERIOR ESTIMATION

Density estimator  $q_{\vec{\lambda}}(\vec{\theta} | \vec{x})$  to approximate  $P(\vec{\theta} | \vec{x})$

- ▶ Typically  $q$  is a (small) neural network, e.g. a normalizing flow

$$\arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\vec{\theta}, \vec{x}) \parallel q_{\vec{\lambda}}(\theta | \vec{x}) P(\vec{x}) \right)$$

Density estimator  $q_{\vec{\lambda}}(\vec{\theta} | \vec{x})$  to approximate  $P(\vec{\theta} | \vec{x})$

- ▶ Typically  $q$  is a (small) neural network, e.g. a normalizing flow

$$\arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\vec{\theta}, \vec{x}) \parallel q_{\vec{\lambda}}(\theta | \vec{x}) P(\vec{x}) \right)$$
$$= \arg \min_{\vec{\lambda}} \int P(\vec{\theta}, \vec{x}) \log \frac{P(\vec{\theta} | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x})} d\vec{\theta} d\vec{x}$$

Density estimator  $q_{\vec{\lambda}}(\vec{\theta} | \vec{x})$  to approximate  $P(\vec{\theta} | \vec{x})$

- ▶ Typically  $q$  is a (small) neural network, e.g. a normalizing flow

$$\begin{aligned} \arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\vec{\theta}, \vec{x}) \parallel q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x}) \right) \\ = \arg \min_{\vec{\lambda}} \int P(\vec{\theta}, \vec{x}) \log \frac{P(\vec{\theta} | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x})} d\vec{\theta} d\vec{x} \\ = \arg \min_{\vec{\lambda}} \int - P(\vec{\theta}, \vec{x}) \log q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) d\vec{\theta} d\vec{x} \end{aligned}$$

Density estimator  $q_{\vec{\lambda}}(\vec{\theta} | \vec{x})$  to approximate  $P(\vec{\theta} | \vec{x})$

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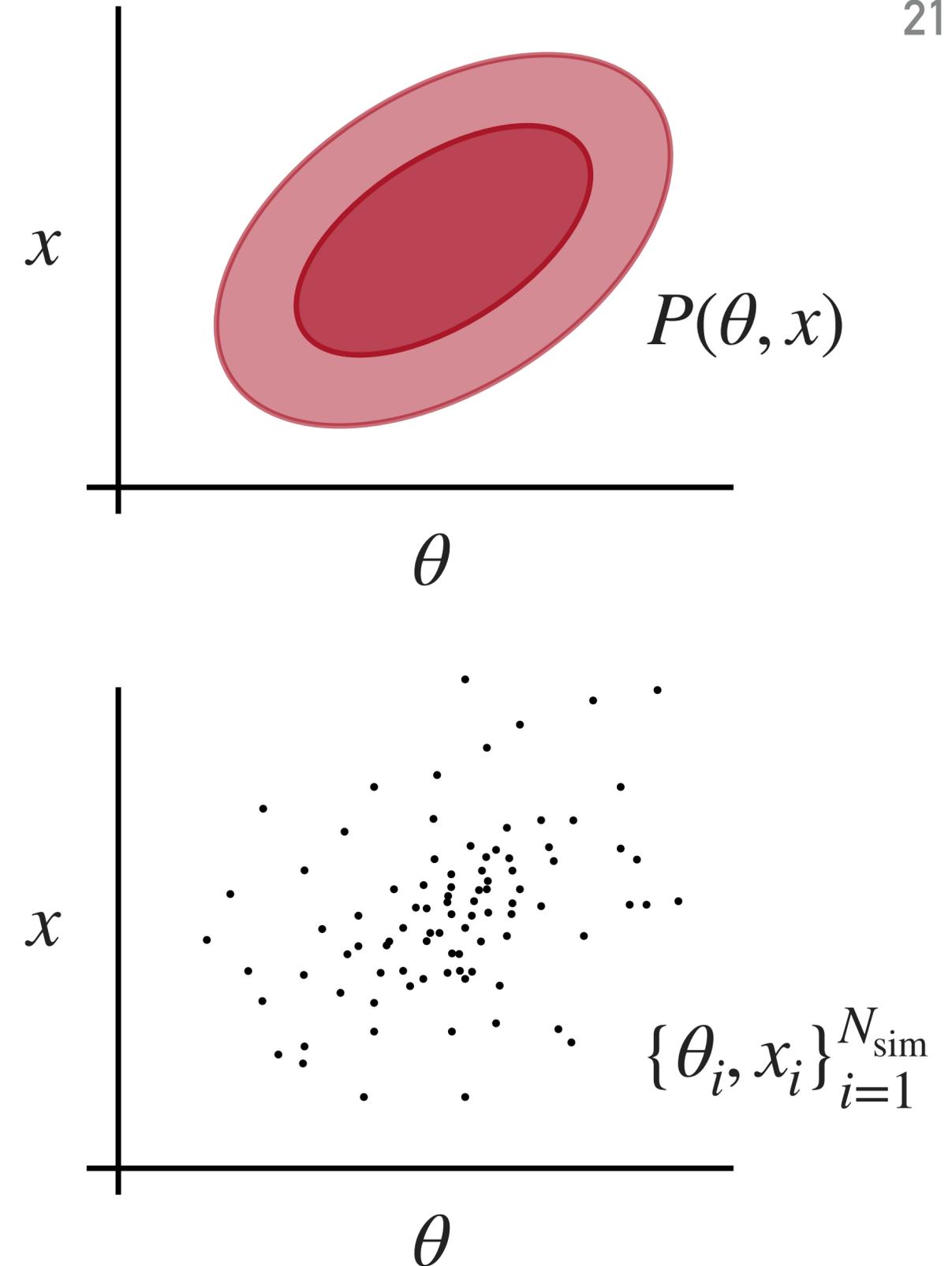
$$\begin{aligned} & \arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\vec{\theta}, \vec{x}) \parallel q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x}) \right) \\ &= \arg \min_{\vec{\lambda}} \int P(\vec{\theta}, \vec{x}) \log \frac{P(\vec{\theta} | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x})} d\vec{\theta} d\vec{x} \\ &= \arg \min_{\vec{\lambda}} \int -P(\vec{\theta}, \vec{x}) \log q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) d\vec{\theta} d\vec{x} \\ &\approx \arg \min_{\vec{\lambda}} \sum_{i=1}^{N_{\text{sim}}} -\log q_{\vec{\lambda}}(\vec{\theta}_i | \vec{x}_i), \text{ sum over } \{\theta_i, x_i\}_{i=1}^{N_{\text{sim}}} \end{aligned}$$

# NEURAL POSTERIOR ESTIMATION

Density estimator  $q_{\vec{\lambda}}(\vec{\theta} | \vec{x})$  to approximate  $P(\vec{\theta} | \vec{x})$

- Typically  $q$  is a (small) neural network, e.g. a normalizing flow

$$\begin{aligned} & \arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\vec{\theta}, \vec{x}) \parallel q_{\vec{\lambda}}(\theta | \vec{x}) P(\vec{x}) \right) \\ &= \arg \min_{\vec{\lambda}} \int P(\vec{\theta}, \vec{x}) \log \frac{P(\vec{\theta} | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x})} d\vec{\theta} d\vec{x} \\ &= \arg \min_{\vec{\lambda}} \int -P(\vec{\theta}, \vec{x}) \log q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) d\vec{\theta} d\vec{x} \\ &\approx \arg \min_{\vec{\lambda}} \sum_{i=1}^{N_{\text{sim}}} -\log q_{\vec{\lambda}}(\vec{\theta}_i | \vec{x}_i), \text{ sum over } \{\theta_i, x_i\}_{i=1}^{N_{\text{sim}}} \end{aligned}$$

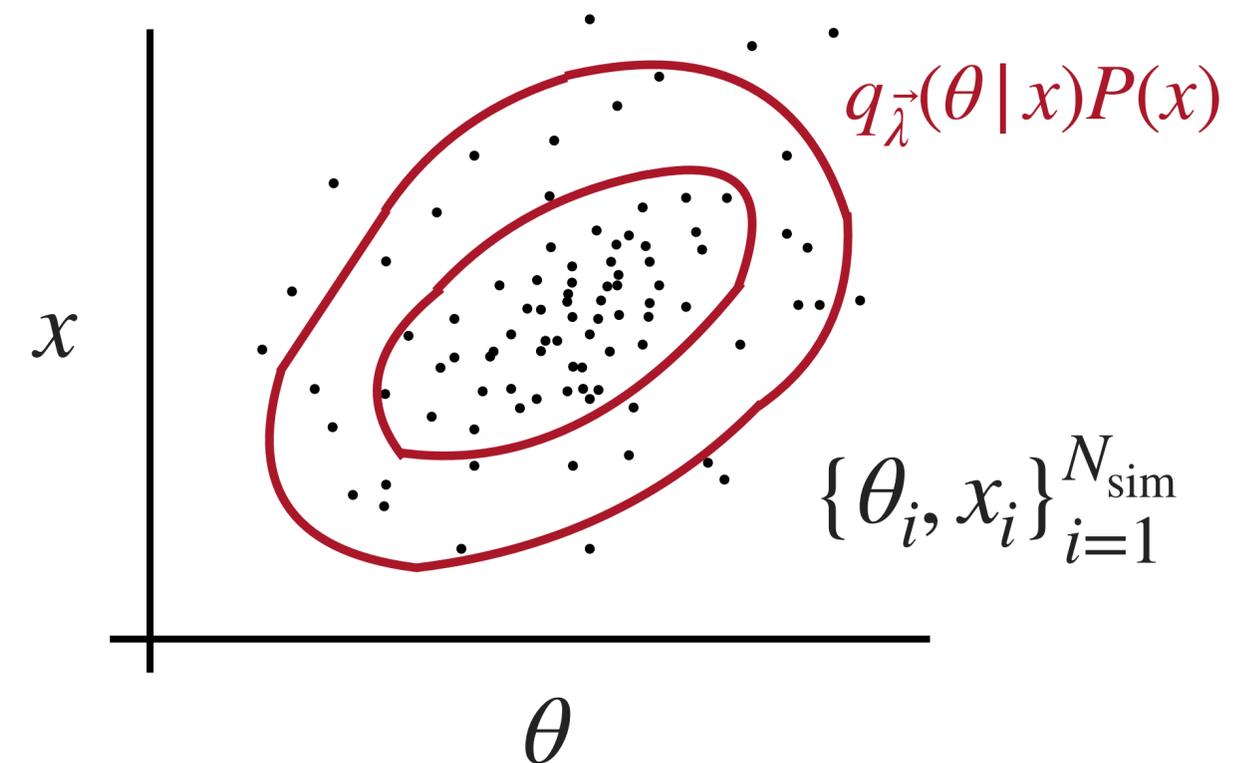
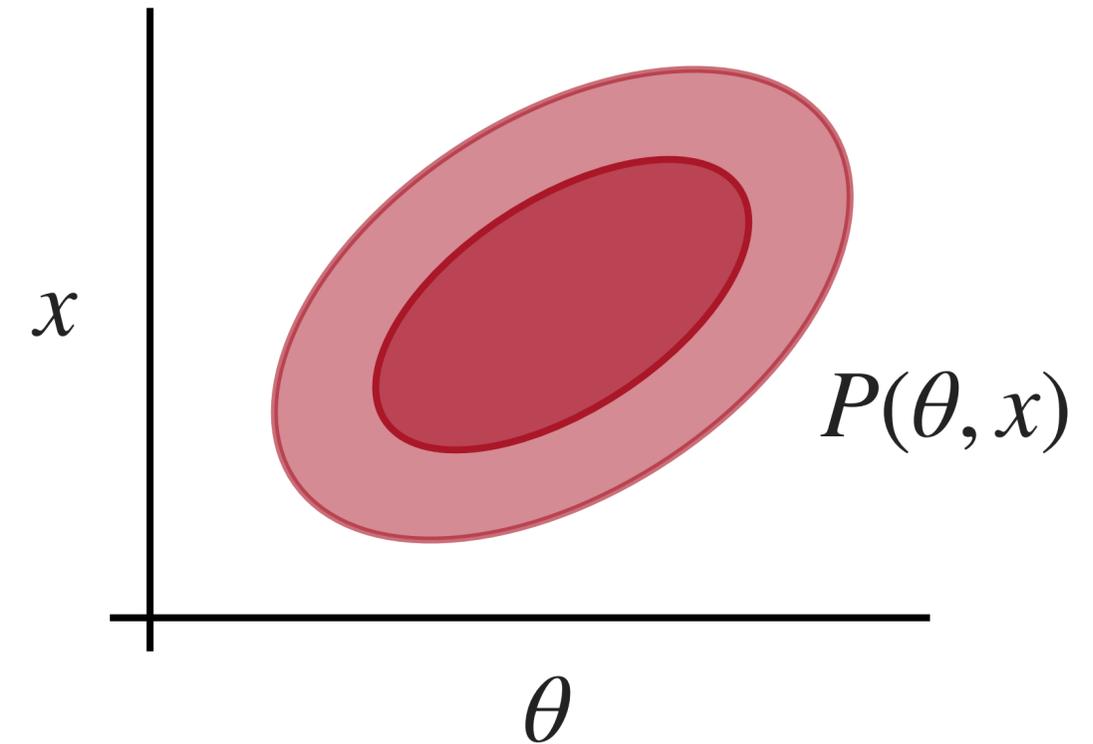


# NEURAL POSTERIOR ESTIMATION

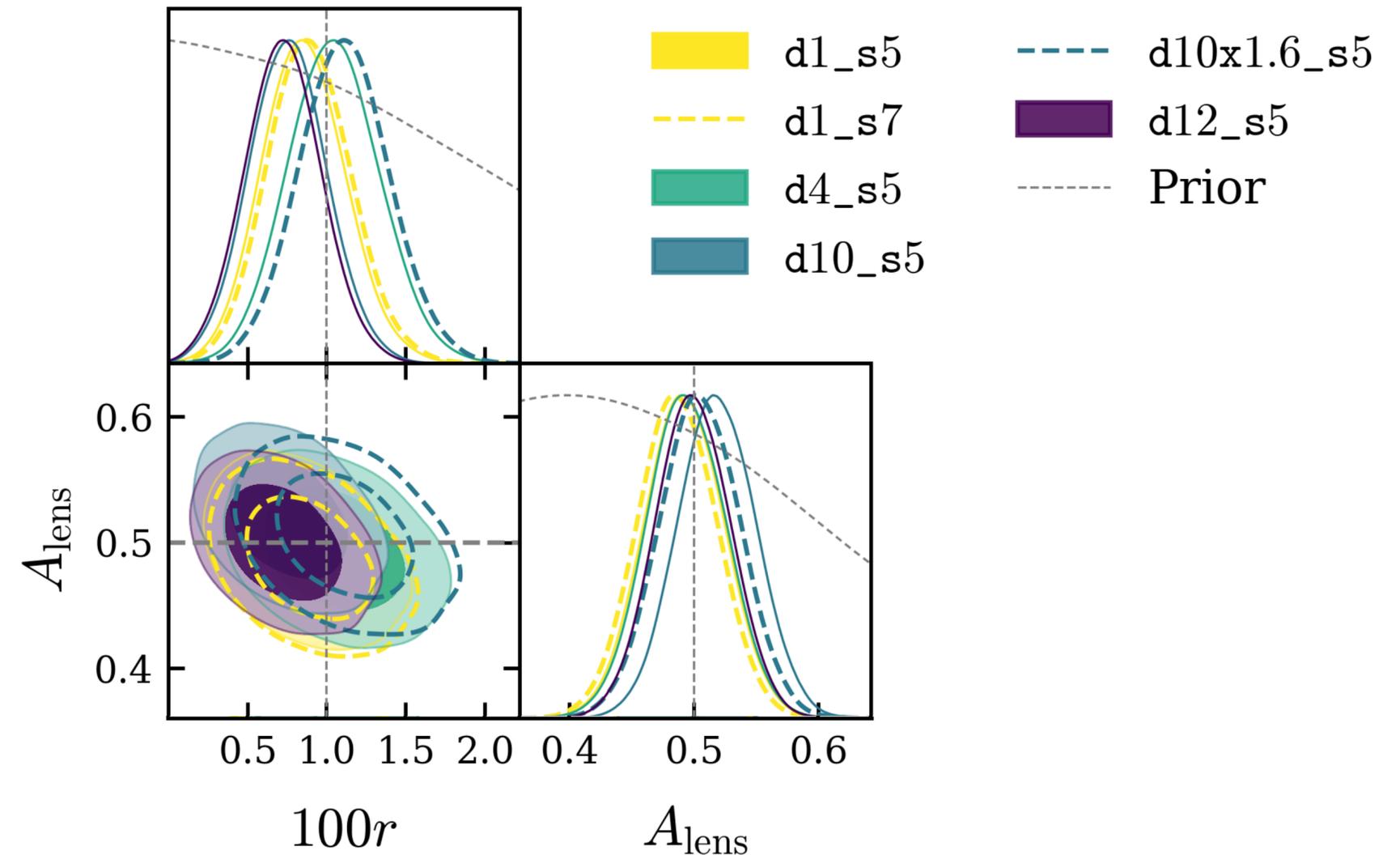
Density estimator  $q_{\vec{\lambda}}(\vec{\theta} | \vec{x})$  to approximate  $P(\vec{\theta} | \vec{x})$

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$$\begin{aligned} & \arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\vec{\theta}, \vec{x}) \parallel q_{\vec{\lambda}}(\theta | \vec{x}) P(\vec{x}) \right) \\ &= \arg \min_{\vec{\lambda}} \int P(\vec{\theta}, \vec{x}) \log \frac{P(\vec{\theta} | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) P(\vec{x})} d\vec{\theta} d\vec{x} \\ &= \arg \min_{\vec{\lambda}} \int -P(\vec{\theta}, \vec{x}) \log q_{\vec{\lambda}}(\vec{\theta} | \vec{x}) d\vec{\theta} d\vec{x} \\ &\approx \arg \min_{\vec{\lambda}} \sum_{i=1}^{N_{\text{sim}}} -\log q_{\vec{\lambda}}(\vec{\theta}_i | \vec{x}_i), \text{ sum over } \{\theta_i, x_i\}_{i=1}^{N_{\text{sim}}} \end{aligned}$$



- ▶ Unbiased  $r$  inference with complicated foregrounds using SBI trained on very simple foreground simulations
- ▶ Exploits SBI's ability to do inference with aggressively compressed data vectors

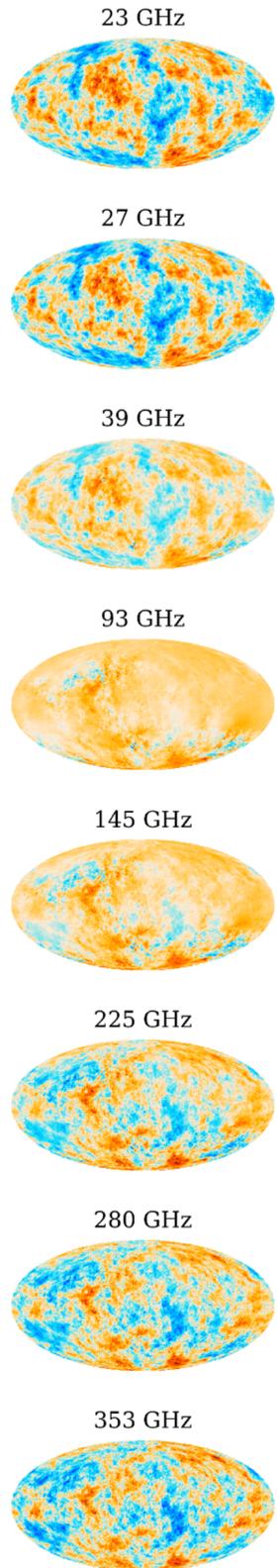


AJD, K. Surrao, A. E. Bayer, A. E. Adler,  
N. Dachlythra, S. Azzoni and J. C. Hill  
(2512.16869)

# GENERATING

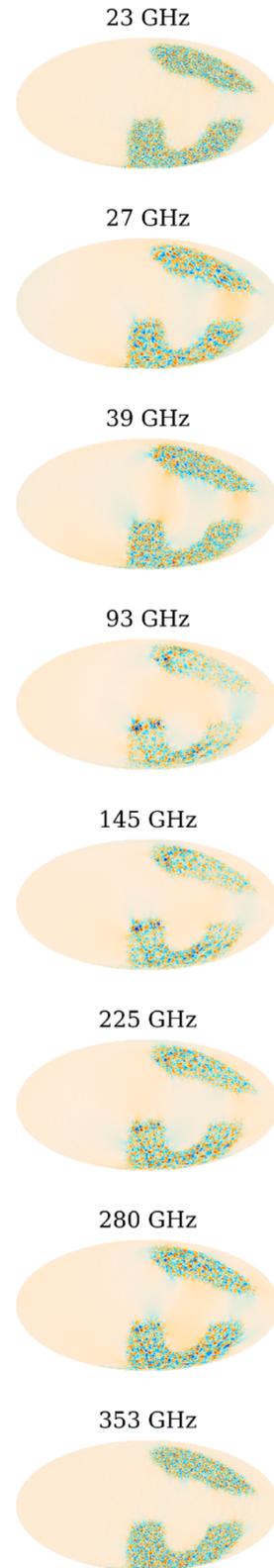
$$\{\vec{\theta}_i, \vec{x}_i\}_{i=1}^{N_{\text{sim}}}$$

$$\vec{\phi}_i \sim P(\vec{\phi} | \vec{\theta}_i)$$



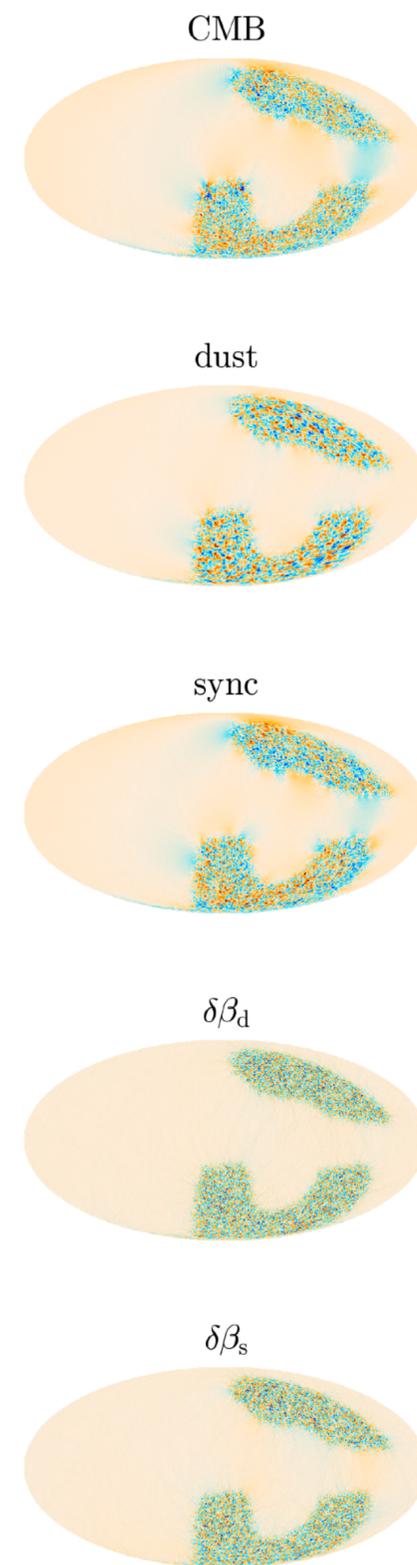
Draw sky realization

$$\vec{d}_i \sim P(\vec{d} | \vec{\phi}_i)$$



Convolve with beam, filter, add noise, mask

$$\vec{x}_i = f(\vec{d}_i)$$



$$\left\{ \begin{array}{l} \hat{C}_\ell^{\text{CMB} \times \text{CMB}} \\ \hat{C}_\ell^{\text{CMB} \times \text{dust}} \\ \vdots \\ \hat{C}_\ell^{\text{sync} \times \delta\beta_s} \\ \hat{C}_\ell^{\delta\beta_s \times \delta\beta_s} \end{array} \right\}$$

15 spectra,  
165 bins total

# NUISANCE PARAMETERS IN SBI

Consider parameter of interest  $\theta_1$  and nuisance parameter  $\theta_2$

▶ We directly target  $P(\theta_1 | \vec{x}) = \int d\theta_2 P(\theta_1, \theta_2 | \vec{x})$

$$\arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\theta_1 | \vec{x}) P(\vec{x}) \parallel q_{\vec{\lambda}}(\theta_1 | \vec{x}) P(\vec{x}) \right)$$

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$$\begin{aligned} \arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\theta_1 | \vec{x}) P(\vec{x}) \parallel q_{\vec{\lambda}}(\theta_1 | \vec{x}) P(\vec{x}) \right) \\ = \arg \min_{\vec{\lambda}} \int P(\theta_1 | \vec{x}) P(\vec{x}) \log \frac{P(\theta_1 | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\theta_1 | \vec{x}) P(\vec{x})} d\theta_1 d\vec{x} \end{aligned}$$

Consider parameter of interest  $\theta_1$  and nuisance parameter  $\theta_2$

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Consider parameter of interest  $\theta_1$  and nuisance parameter  $\theta_2$

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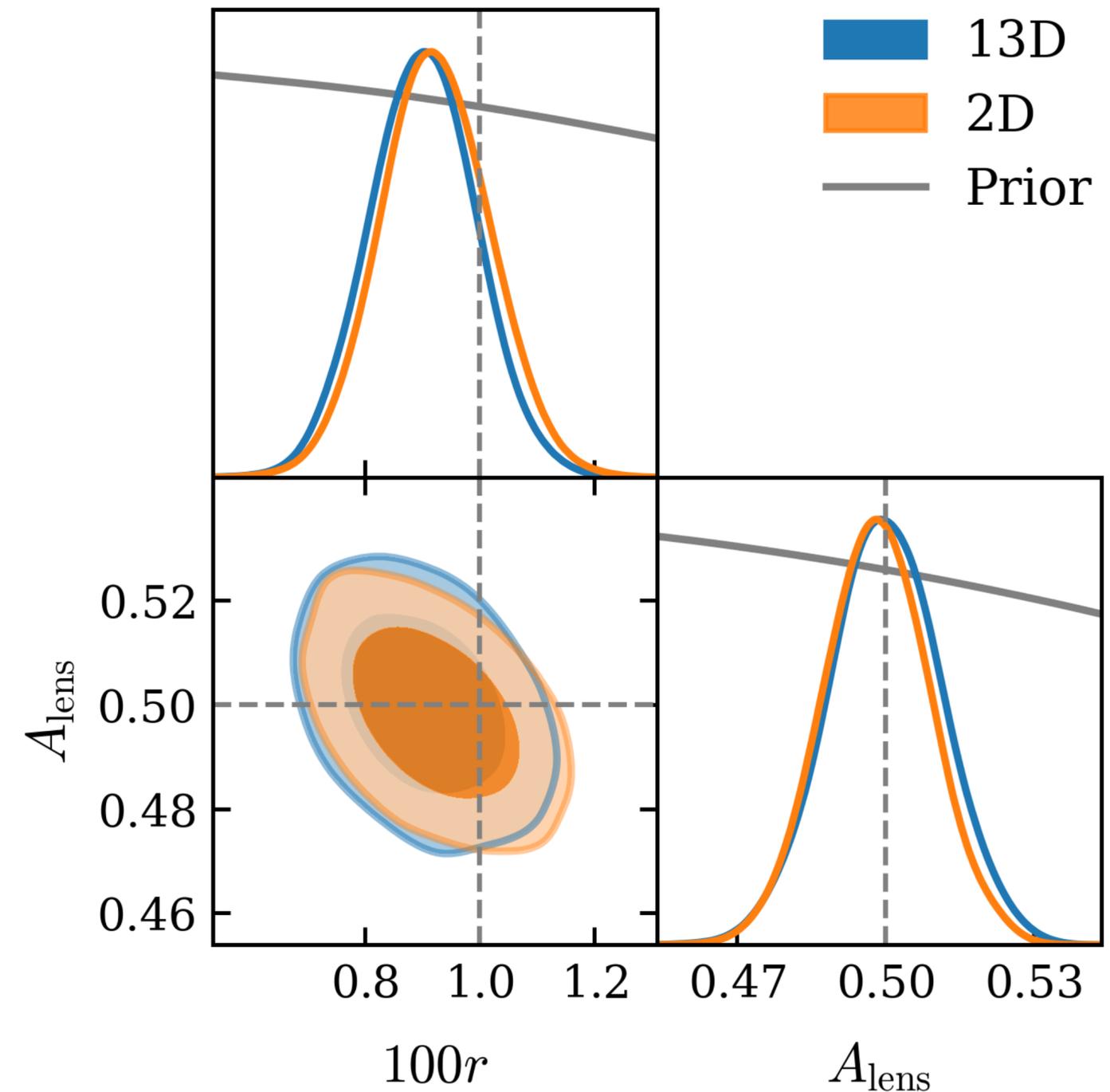
$$\begin{aligned} & \arg \min_{\vec{\lambda}} D_{\text{KL}} \left( P(\theta_1 | \vec{x}) P(\vec{x}) \parallel q_{\vec{\lambda}}(\theta_1 | \vec{x}) P(\vec{x}) \right) \\ &= \arg \min_{\vec{\lambda}} \int P(\theta_1 | \vec{x}) P(\vec{x}) \log \frac{P(\theta_1 | \vec{x}) P(\vec{x})}{q_{\vec{\lambda}}(\theta_1 | \vec{x}) P(\vec{x})} d\theta_1 d\vec{x} \\ &= \arg \min_{\vec{\lambda}} \int -P(\theta_1, \theta_2, \vec{x}) \log q_{\vec{\lambda}}(\theta_1 | \vec{x}) d\theta_1 d\theta_2 d\vec{x} \\ &\approx \arg \min_{\vec{\lambda}} \sum_{i=1}^{N_{\text{sim}}} -\log q_{\vec{\lambda}}(\vec{\theta}_{1,i} | \vec{x}_i), \text{ sum over } \{\theta_{1,i}, x_i\}_{i=1}^{N_{\text{sim}}} \end{aligned}$$

# NUISANCE PARAMETERS

- ▶ With SBI, including nuisance parameters is straightforward
- ▶ Define prior distribution of additional parameters and includes their effect in the simulations
- ▶ No architectural changes to the normalizing flow network are needed, provided it has sufficient capacity

Consistent results for  $r$  and  $A_{\text{lens}}$  regardless of whether the normalizing flow is trained to predict the posterior of all 13 parameters or just  $r$  and  $A_{\text{lens}}$

25



- ▶ With improvements in SNR, we should be careful with modeling errors in the standard CMB data reduction (e.g. mapmaking)
- ▶ The properties of the beam (leakage, polarized components, chromaticity) start to dominate the systematic error budget → Need tailored calibration strategies
- ▶ For certain CMB analyses, e.g.  $B$ -mode searches for  $r$ , simulation-based inference provides a promising way to deal with systematics