

MAX-PLANCK-INSTITUT  
FÜR ASTROPHYSIK



# New standard ingredients in cosmological analyses?

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# Context

- **Inflation:** reconstruct the properties of the initial conditions, and look for gravitational waves  $f_{\text{NL}}$   
 $n_s, r$
- **Dark Energy and Gravity:** the growth of structure depends sensitively on the **expansion history** of the Universe, and the nature of **gravity**  
 $w_0, w_a, f \propto D'/D$   
Growth equation:  $D'' + aH D' = 4\pi G \bar{\rho} D$
- **Dark Matter/neutrinos:** how “cold” is cold dark matter ? What is the sum of neutrino masses ?  $\sum m_\nu$

# Context

- **Inflation:** reconstruct the properties of the initial conditions, and look for gravitational waves  $f_{\text{NL}}$   
 $n_s, r$

- **Dark Energy** How should we do inference in this space? expansion

hist What to vary, what to keep fixed?  $f$   
gravity  $w_0, w_a, f \propto D'/D$

Growth equation:  $D'' + aHD' = 4\pi G \bar{\rho} D$

- **Dark Matter/neutrinos:** how “cold” is cold dark matter ? What is the sum of neutrino masses ?  $\sum m_\nu$

# The standard model of cosmology

- (Euclidean)  $\Lambda$ CDM

$$\omega_c, \omega_b, M_\nu, h, A_s, n_s, (\Omega_\Lambda)$$

- not counting astrophysics parameters

- **Assumptions/issues:**

- Assume *simple inflation* prior (Euclidean; scale-invariant  $P_R(k)$ ; purely adiabatic perturbations)
- We don't really know what we are parametrizing with  $\omega_c$
- Assume cosmological constant
- Assume specific neutrino mass ordering

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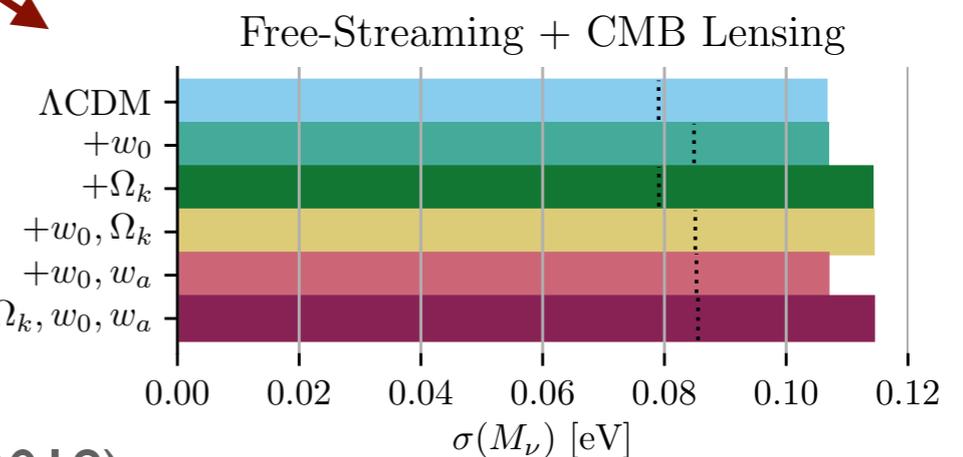
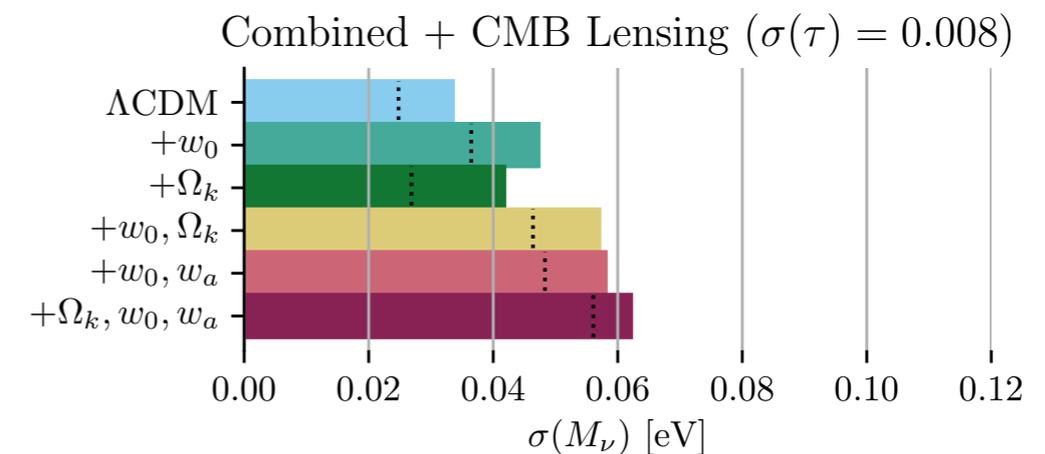
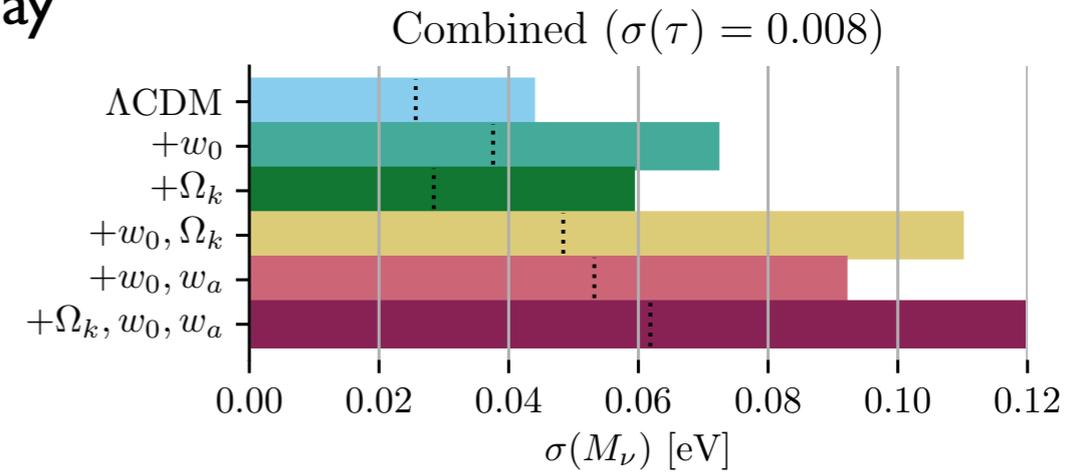
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# Neutrino masses

Forecast

Cf. discussion on Monday

- Part of the standard model — but current  $M_\nu$  constraints sensitive to model extensions
- Model-independent constraints possible using scale-dependent suppression, but these are much weaker and will remain so for some time



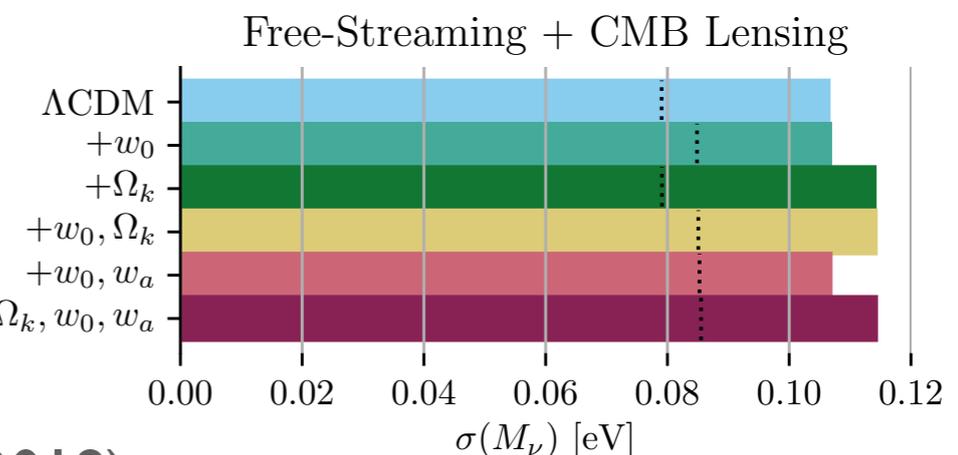
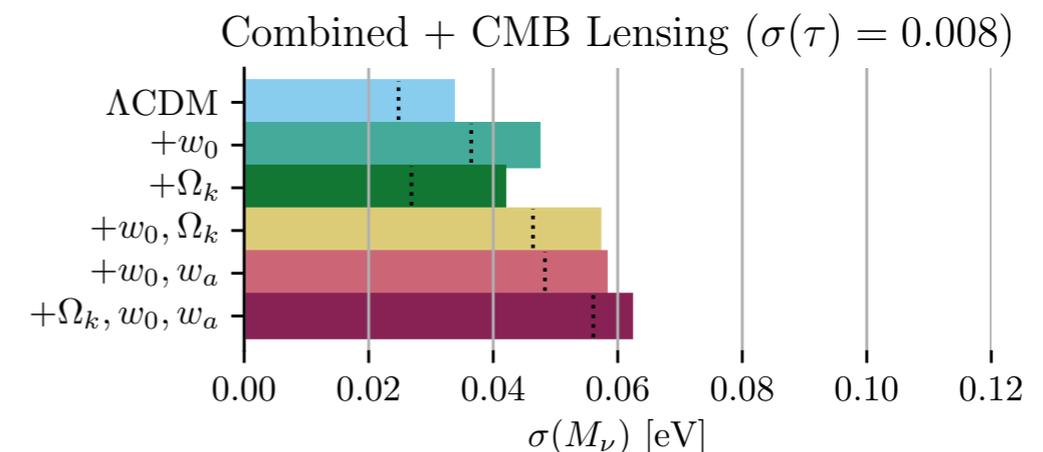
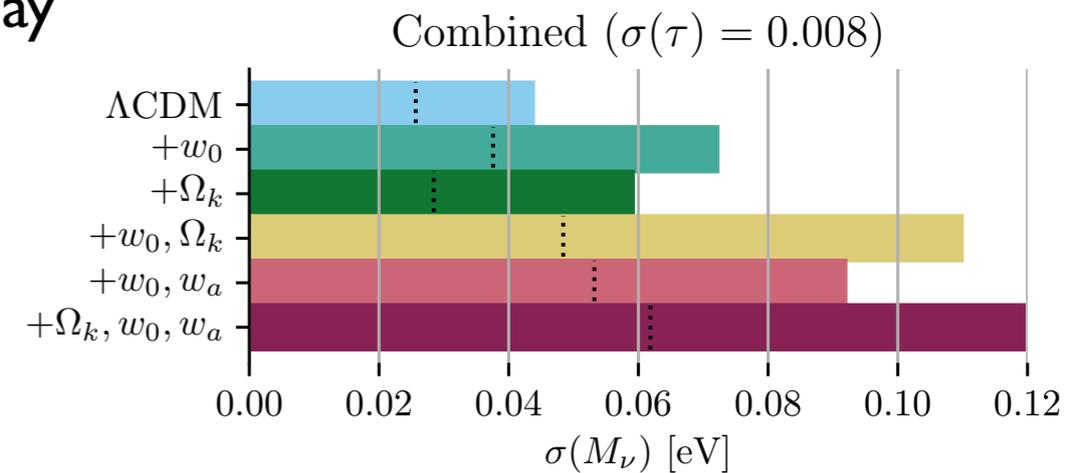
Boyle & FS (2020)  
 Boyle (2018)  
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- Sources of constraint depend strongly on details of dataset combination — lots of possibilities for confusion; clear and careful phrasing essential
  - Also prior dependence...



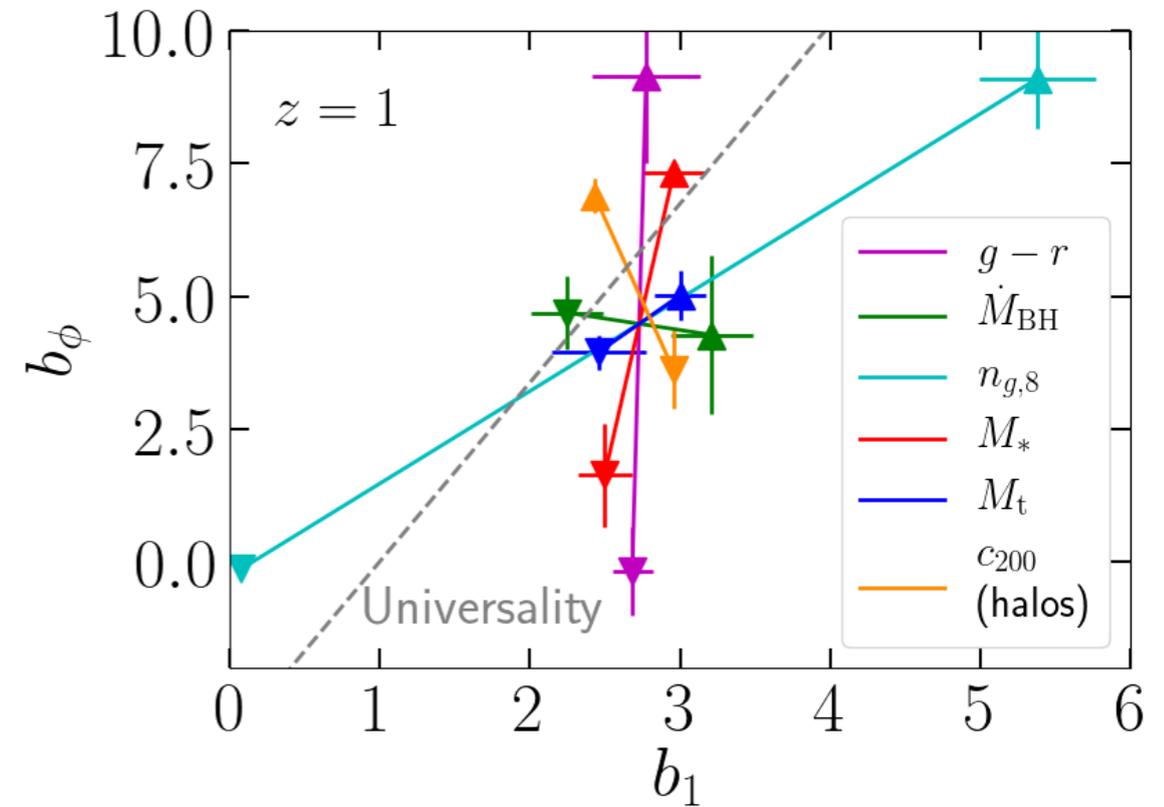
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# Inflation: CMB

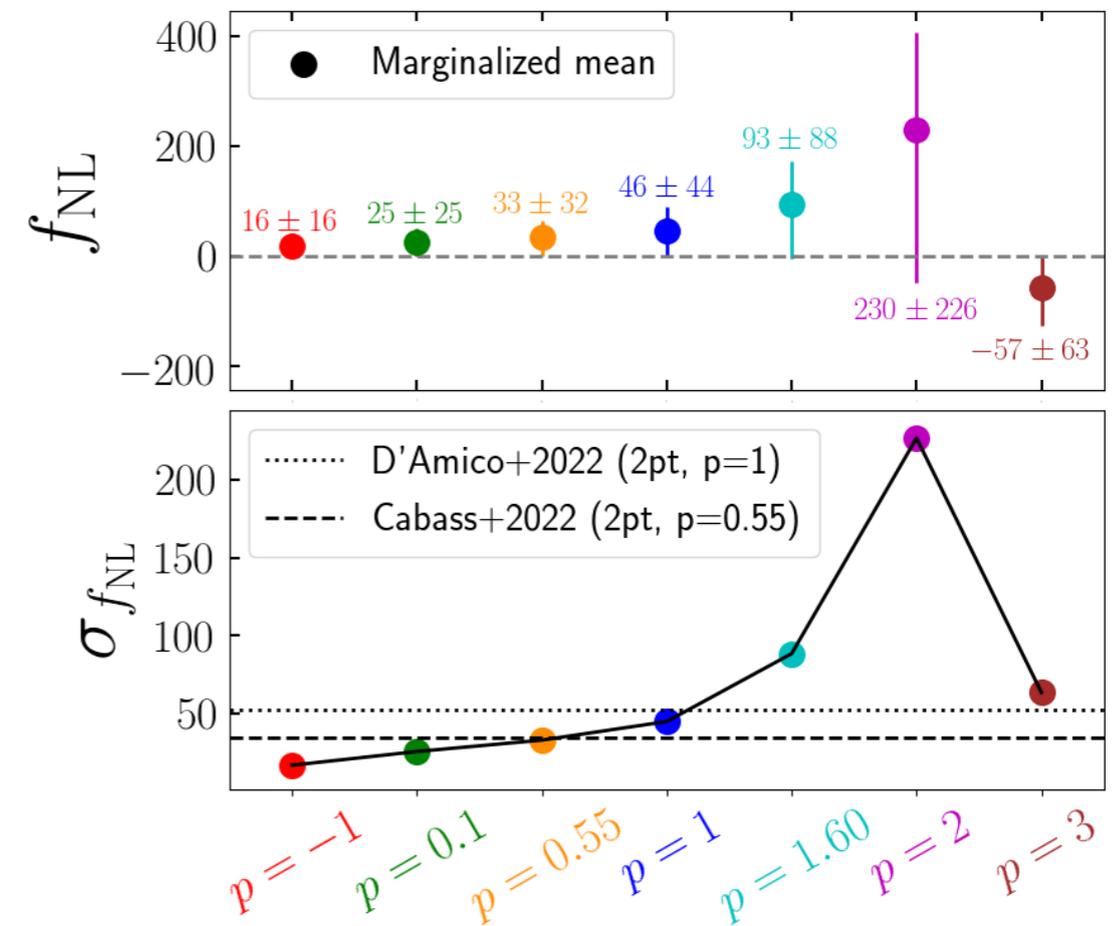
- We need to assume some form of prior in model space
- Luckily, inflation scenarios *largely* divide into two classes (*Braglia*):
  - Single dominant d.o.f.:  $r$  potentially detectable;  $f_{\text{NL}}^{\text{loc}}=0$
  - $> 1$  light d.o.f. which mix:  $r \sim 0$ ;  $f_{\text{NL}}^{\text{loc}}$  detectable
- Fine to ignore  $f_{\text{NL}}$  in  $n_s$ - $r$  constraints
- CMB: template correlations in PNG searches need to be considered
  - cf.  $f_{\text{NL}}^{\text{ortho}}$  in EFT of single-field inflation
  - quasi-single-field / collider signatures

# Inflation: LSS

- Current  $f_{\text{NL}}^{\text{loc}}$  constraints from LSS (scale-dependent bias) fix  $\Lambda\text{CDM}$  parameters and  $b_\phi$ , where the data constrain only  $b_\phi * f_{\text{NL}}^{\text{loc}}$
- This really is no longer ok...
- Of these,  $b_\phi$  is the more difficult problem; we need informative priors to obtain constraints on  $f_{\text{NL}}^{\text{loc}}$
- Issue also in kSZ, measuring momentum of ionized gas (biased)
- More work needed!



Barreira, Krause (2023)  
Barreira (2022), ...

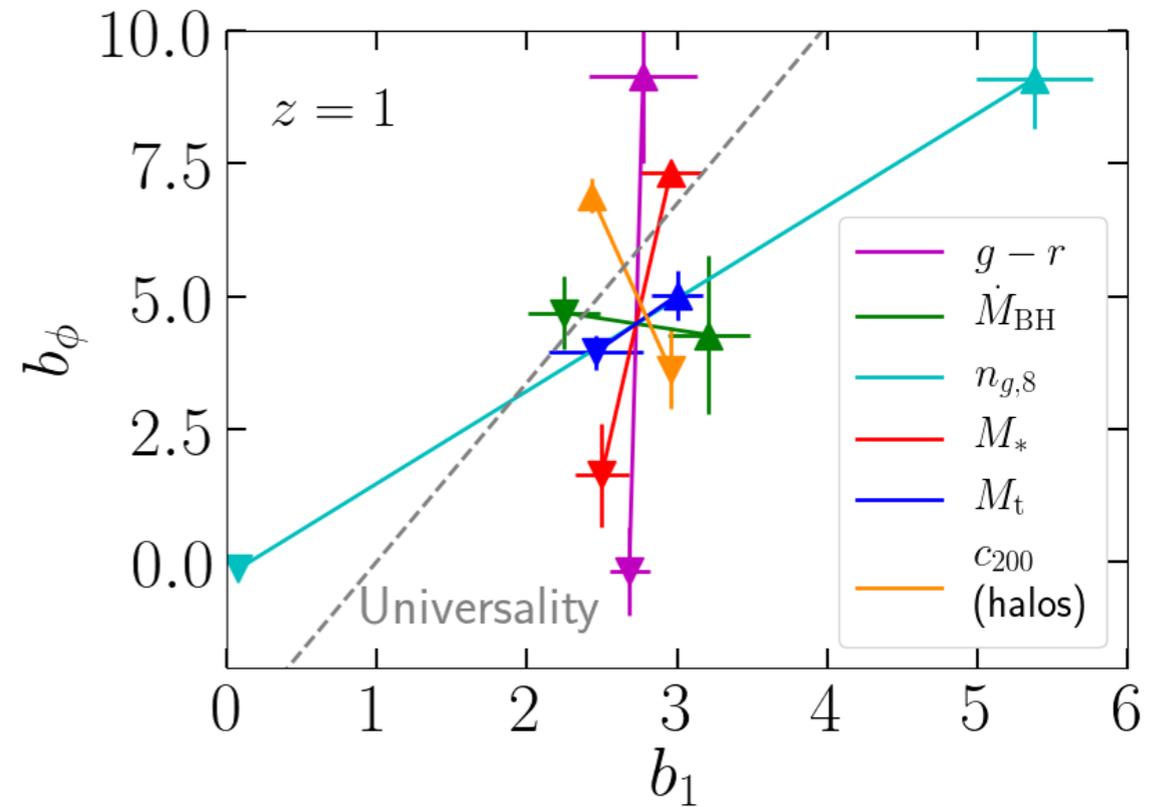


# Inflation: LSS

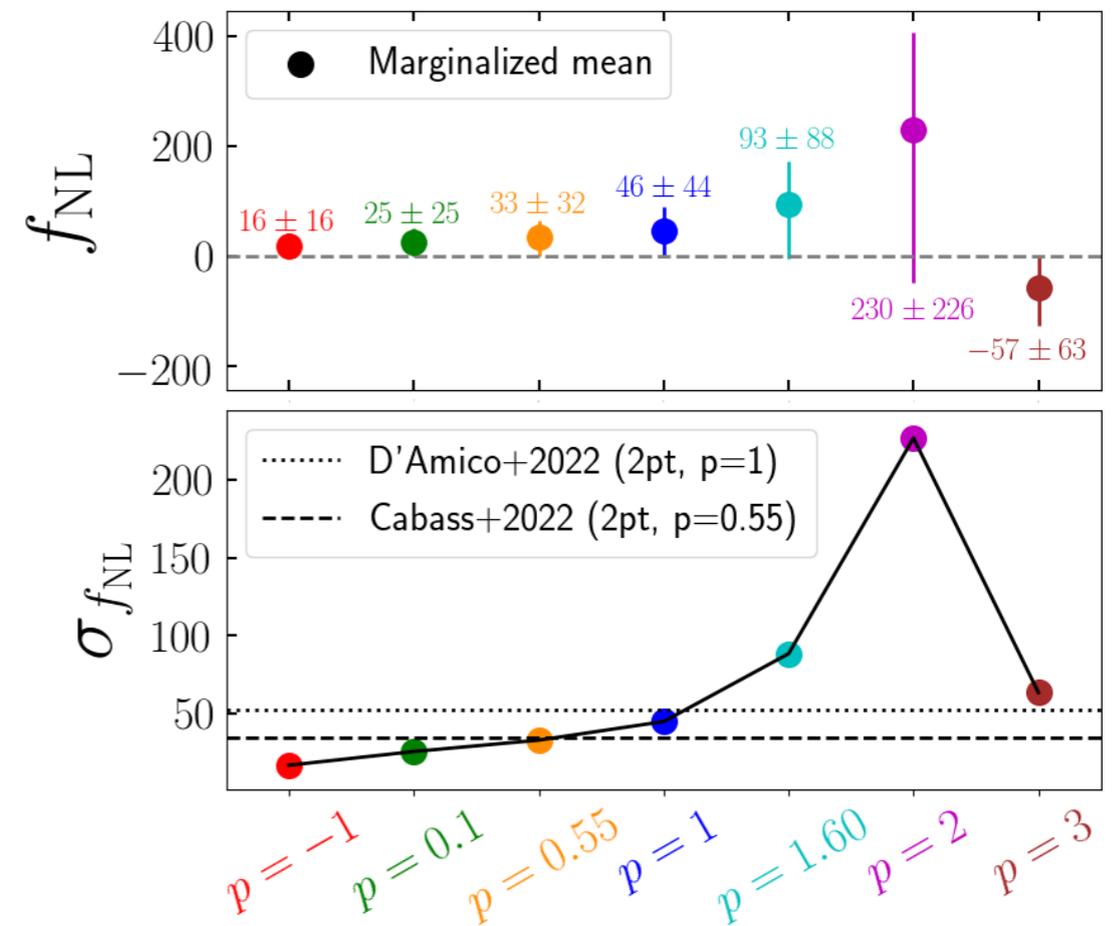
- Moreover,  $f_{\text{NL}}^{\text{loc}}$  signature *exactly degenerate* with  $g_{\text{NL}}^{\text{loc}}$  and compensated isocurvature modes

Desjacques, Ferraro, LoVerde, Smith, ...  
Barreira, Cabass, FS, ...

- Both expected in general for multifield inflation



Barreira, Krause (2023)  
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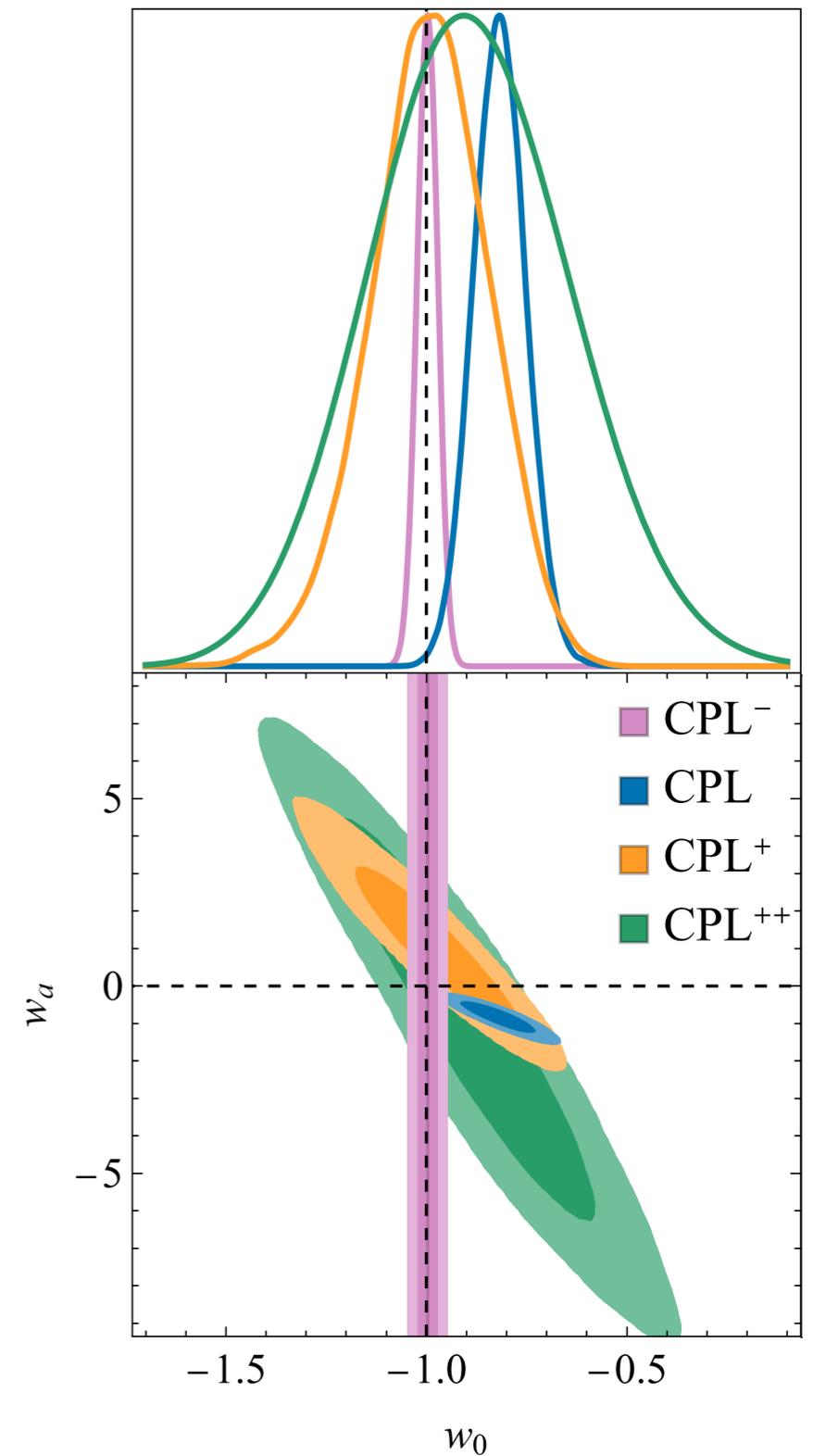


# Dark Energy

- How to parametrize dark energy beyond  $\Lambda$ ?
  - Consider concrete models
  - Parametrize equation of state
- Both have issues:
  - Simple quintessence models possibly too restrictive  $\longrightarrow$  *Baker*; see below
  - Parametrization like  $w_0, w_a$  can only be trusted over limited redshift interval

# On $w_0$ - $w_a$

- Parametrization like  $w_0, w_a$  can only be trusted over limited redshift interval
- Best constraints on DE from  $d_A(z)$ 
  - $w_0 \sim d_A''$  ;  $w_a \sim d_A'''$  (!)
  - If  $w_a \sim 1$ , expect  $w_{aa} \sim 1$  as well, but almost all analyses fix it to 0...



$$w_{\text{DE}}(a) = w_0 + w_a(1-a) + w_b(1-a)^2 + w_c(1-a)^3$$

# Dark Energy *can* cross phantom divide

- If observations indicate  $w$  goes below  $-1$ , have we ruled out “ordinary” dark energy?

- Canonical scalar field: yes

$$p(\phi) = X + V(\phi) \quad \Rightarrow \quad w = \frac{\dot{\phi}^2/2 - V(\phi)}{\dot{\phi}^2/2 + V(\phi)}$$

$$X \equiv -\frac{1}{2}(\partial_\mu\phi)^2$$

- Not true in general: could have equation of state that *varies around*  $w=-1$

- **Monodromic  $k$ -essence:**  $p(\phi, X) = \tilde{V}(\phi) [-X/M^4 + (X/M^4)^2]$

$$\tilde{V}(\phi) = C \left( \frac{\phi}{\phi_0} \right)^{-\alpha} [1 - A \sin(\nu H_0 \phi + \delta)].$$

# Dark Energy *can* cross phantom divide

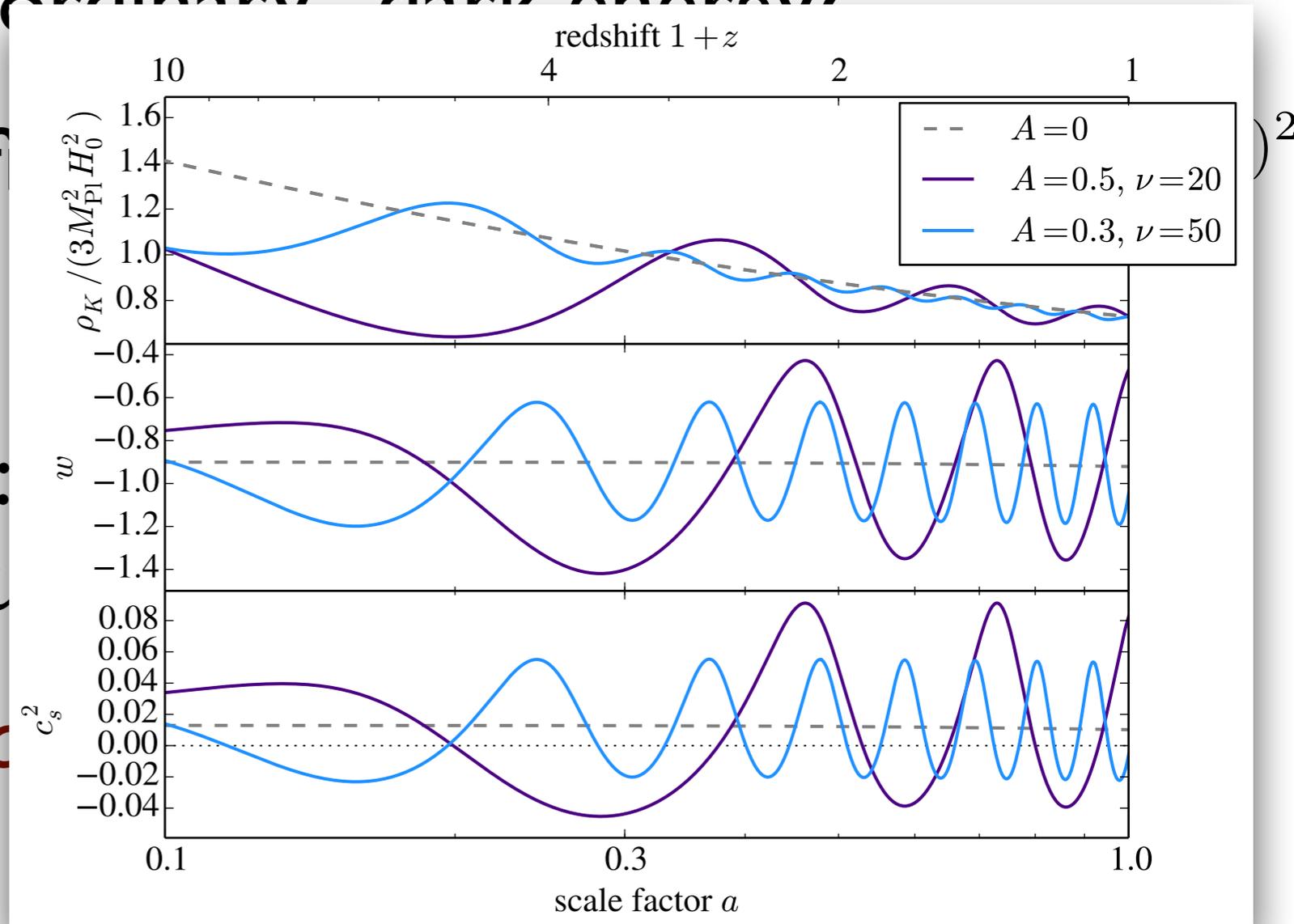
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- *Monodromic k-essence*



# Dark Energy *can* cross phantom divide

- Fine at the background level, but DE perturbations suffer tachyonic instabilities if  $c_s^2 < 0$
- k-essence case naturally has  $c_s^2 \ll 1$ ; in fact,  $c_s^2 \sim (1+w)$  in  $1+w \rightarrow 0$  limit, leading to tachyonic instabilities as  $1+w < 0$

- These can be dealt with consistently if

- Higher-derivative contributions are present:

$$\delta\ddot{\phi} \sim -c_s^2 k^2 \delta\phi + \frac{k^4}{\bar{M}^2} \delta\phi + \dots$$

e.g., from

$$\Delta\mathcal{L}_{\text{DE,h.deriv.}} = -\frac{\bar{M}^2}{2} [\square\phi + 3H(\phi)]^2$$

- $c_s^2$  stays infinitesimally below 0
- Lowers cutoff of the theory, but not ruled out.



# Dark Energy *can* cross phantom divide

- An example viable model (due to Marco Celoria):

$$p(\phi, X) = \frac{\bar{M}^4}{2}(2X - 1)^2 - F(\phi) + G(\phi)(2X + 1)$$

$$F(\phi) = V_0 \left[ 1 - \tilde{A} \sin(\tilde{\nu} H_0 \phi) \right]$$

$$G(\phi) = V_0 \tilde{A} \tilde{\nu} H_0 \cos(\tilde{\nu} H_0 \phi).$$

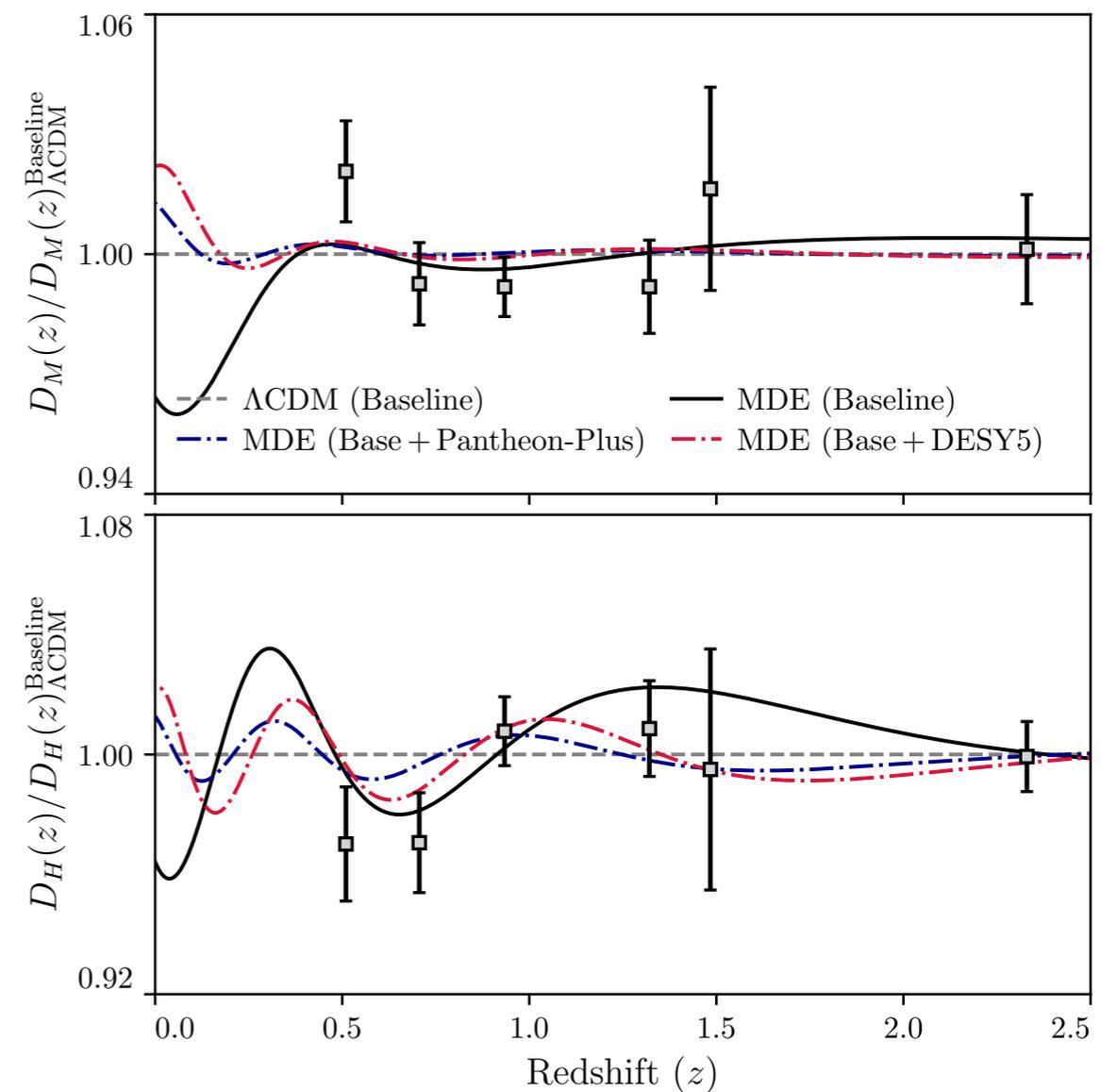
- Oscillations with amplitude  $\Delta w \sim 0.1$  around  $w = -1$  easily possible while satisfying constraints on instabilities and having cutoff  $> \text{eV}$  scale.



# Monodromic k-essence and DESI

Goldstein, Celoria, FS (2025)

- 3 free parameters (FS 2017 model) in addition to  $\Omega_{de}$ , potential tilt  $\alpha \Leftrightarrow$  mean  $w$ :
  - amplitude, frequency, phase of oscillations
- Exclude all observables sensitive to perturbations here

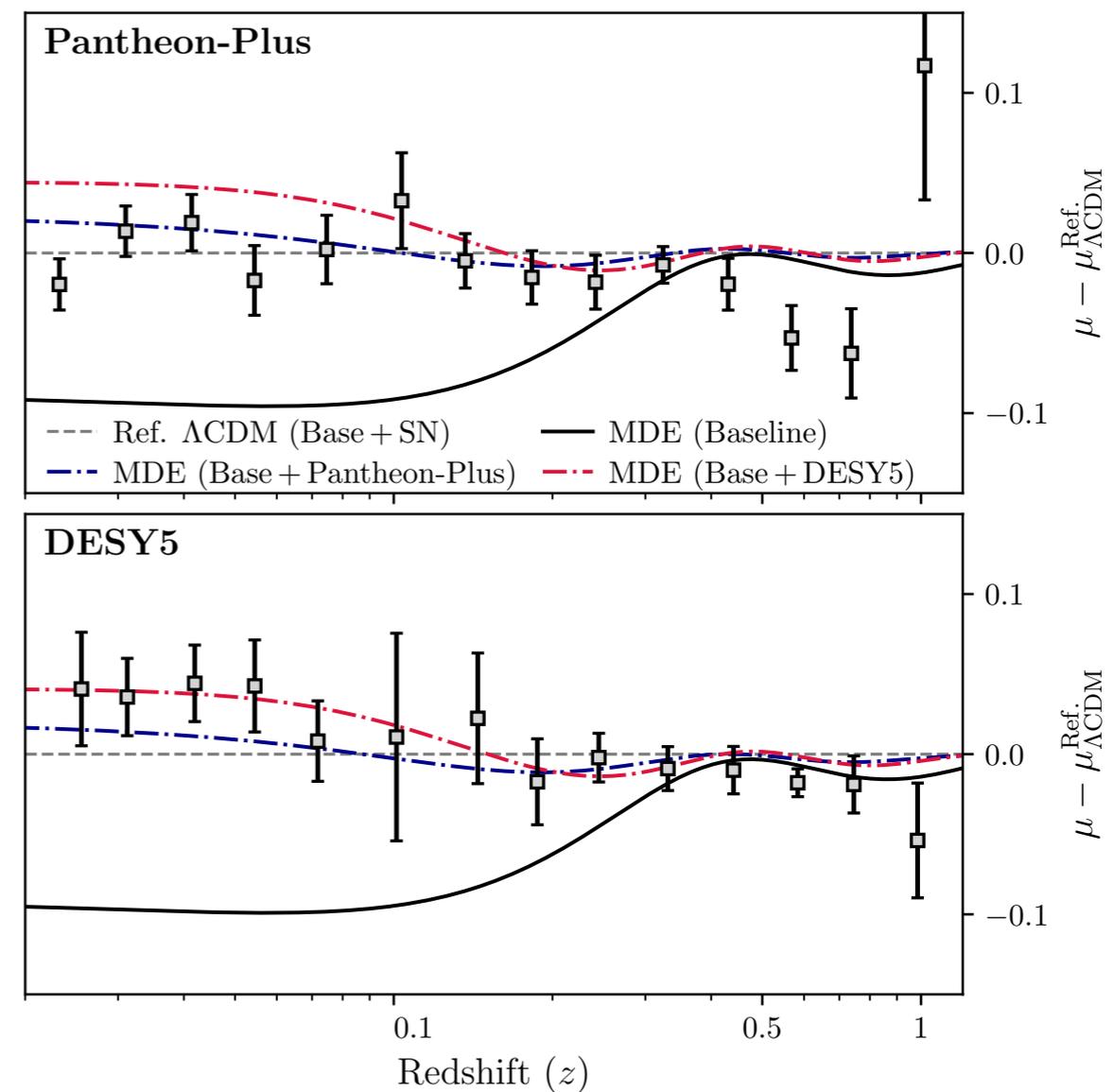




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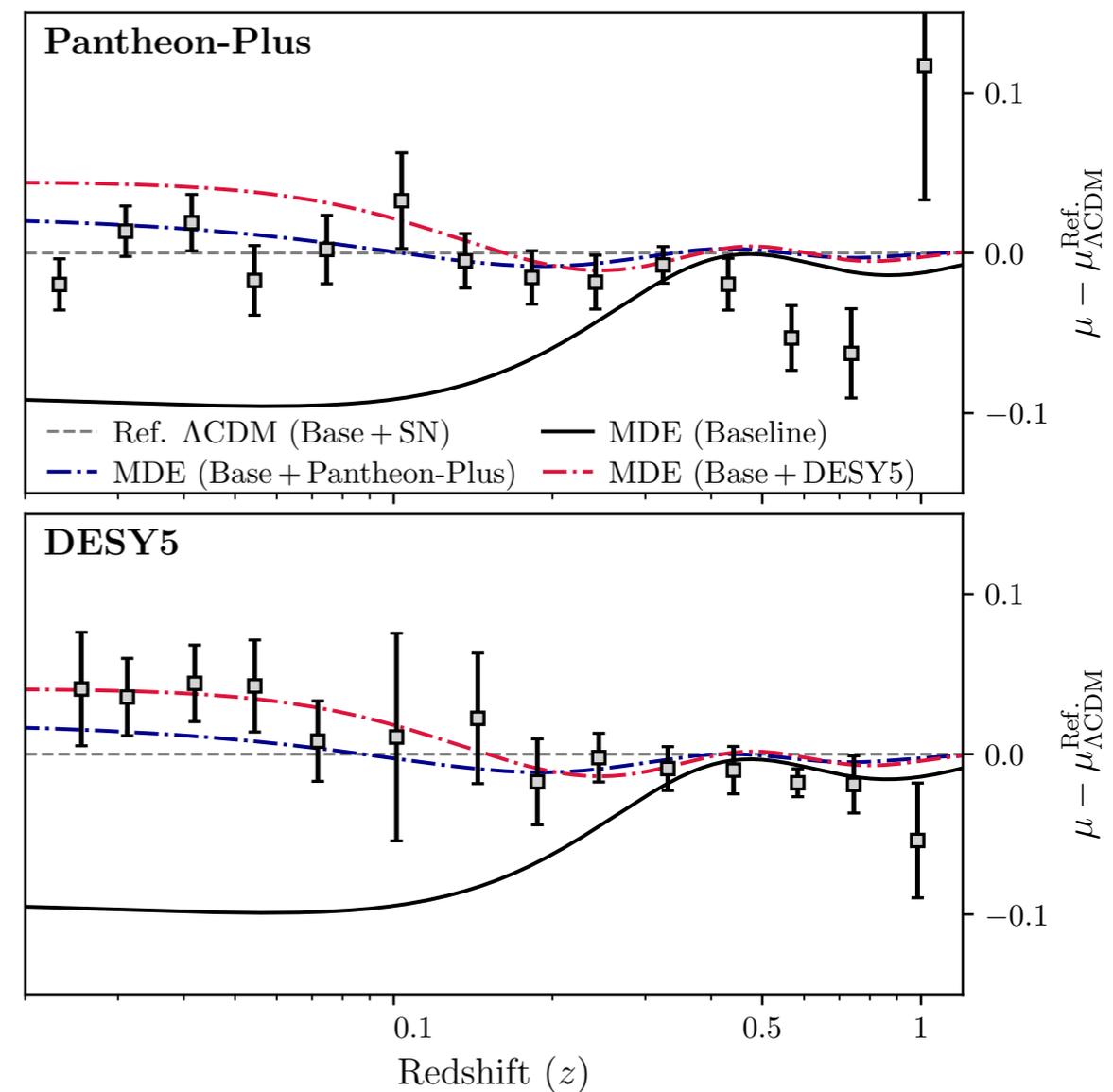




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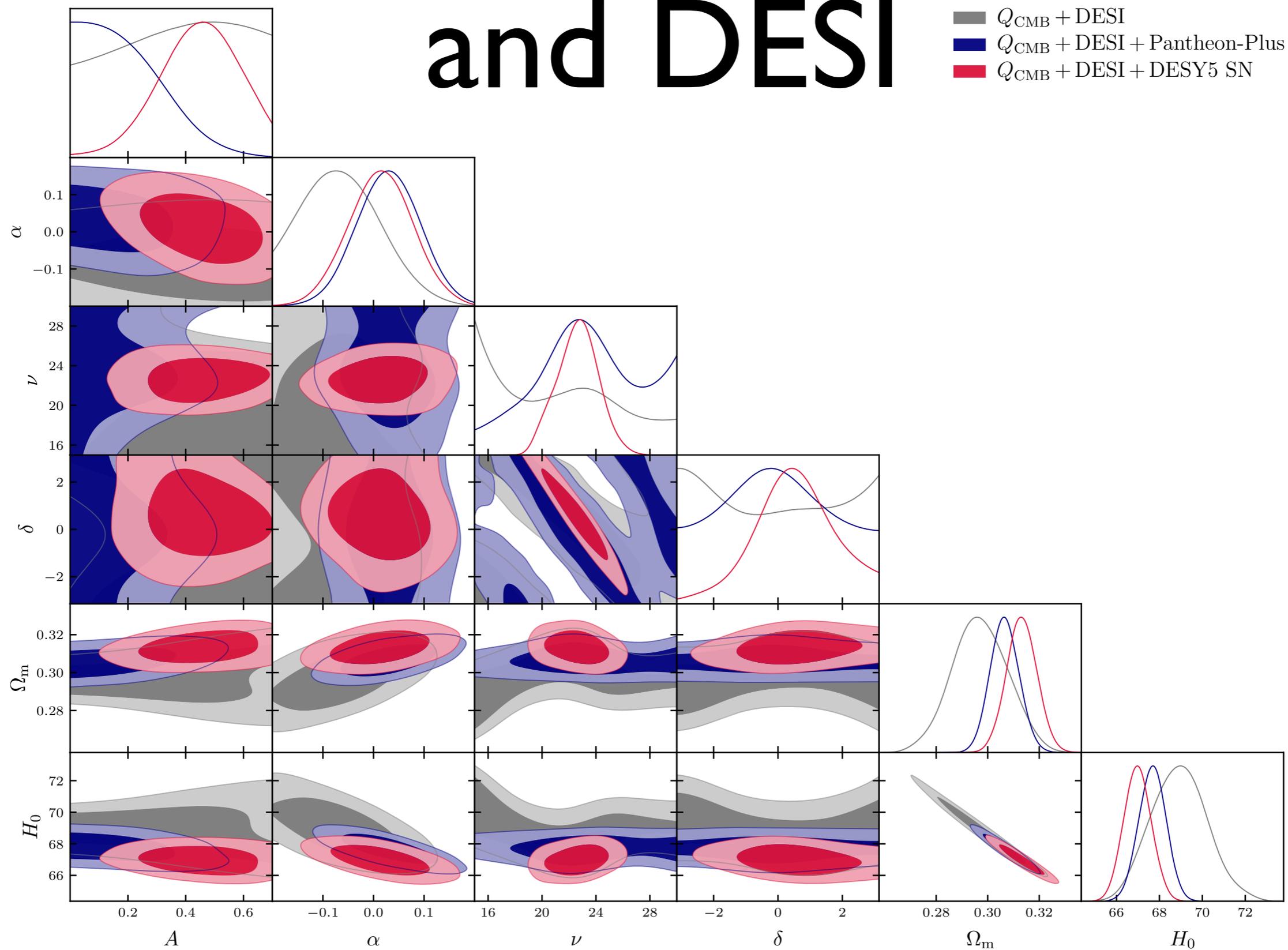
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- 3 free parameters (FS 2017 model) in addition to  $\Omega_{de}$ , potential tilt  $\alpha \Leftrightarrow$  mean  $w$ :
  - amplitude, frequency, phase of oscillations
- Exclude all observables sensitive to perturbations here
- Similar fit quality to DESI BAO + SN as  $w_0, w_a$
- Mean  $w$  consistent with -1 (motivated by theory as well); then, only 1 more free parameter than  $w_0, w_a$  !



# Monodromic k-essence

## and DESI



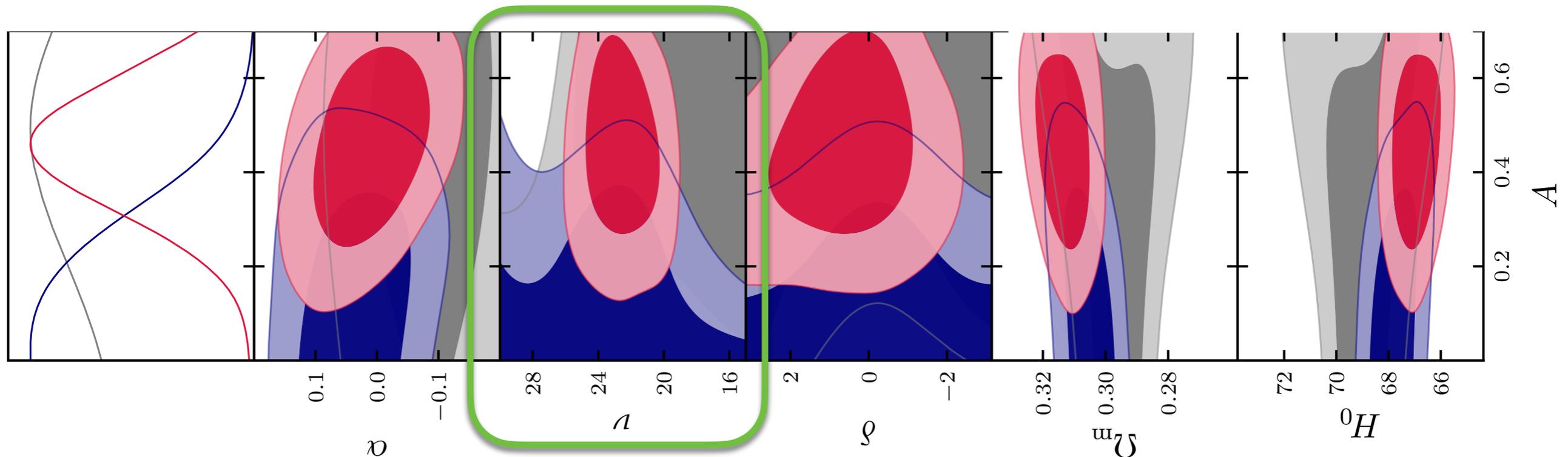


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■  $Q_{CMB} + DESI$   
■  $Q_{CMB} + DESI + Pantheon-Plus$   
■  $Q_{CMB} + DESI + DESY5 SN$

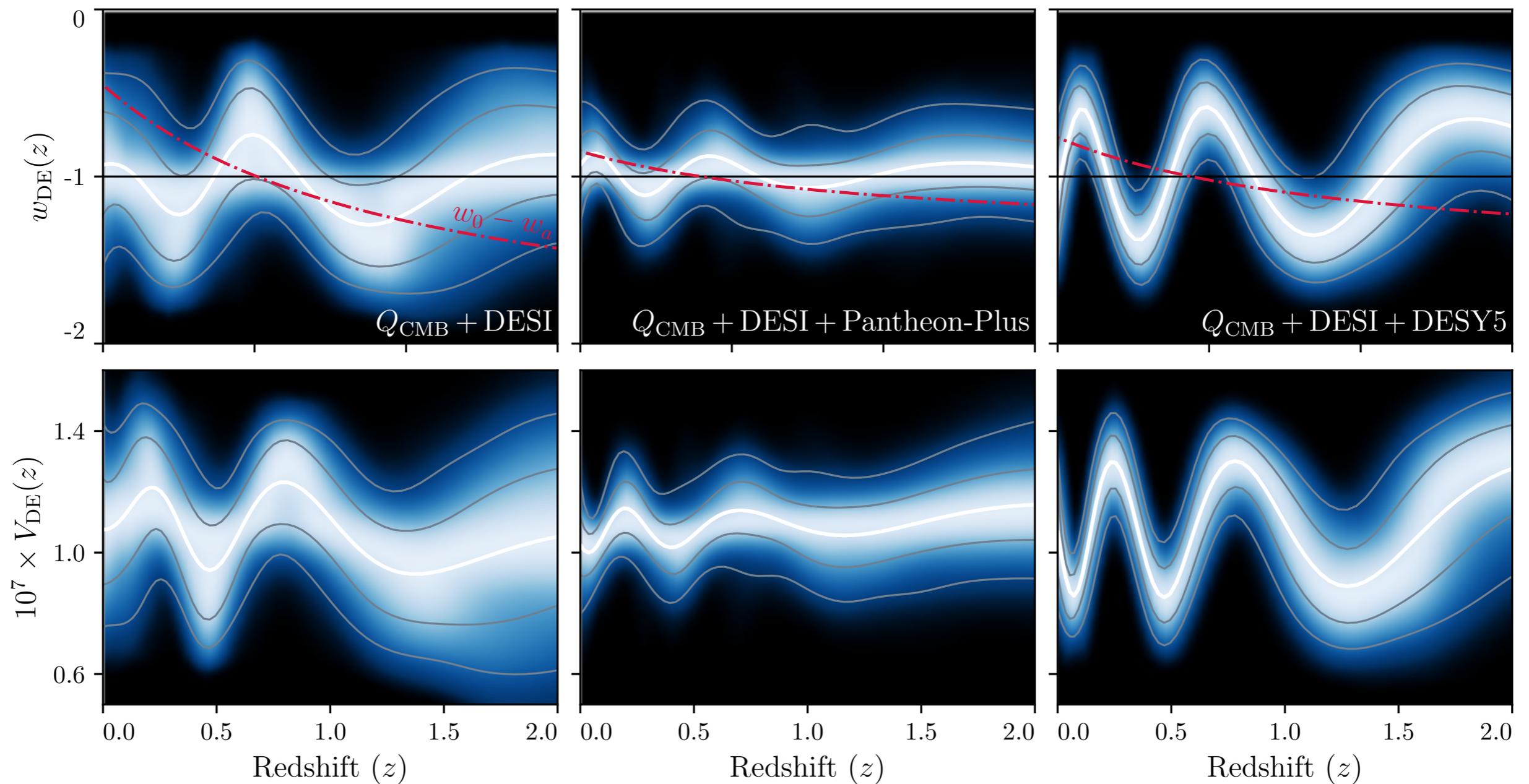




Goldstein, Celoria, FS (2025)

# Monodromic k-essence and DESI

- Reconstruction of  $w(z)$  and k-essence “potential”



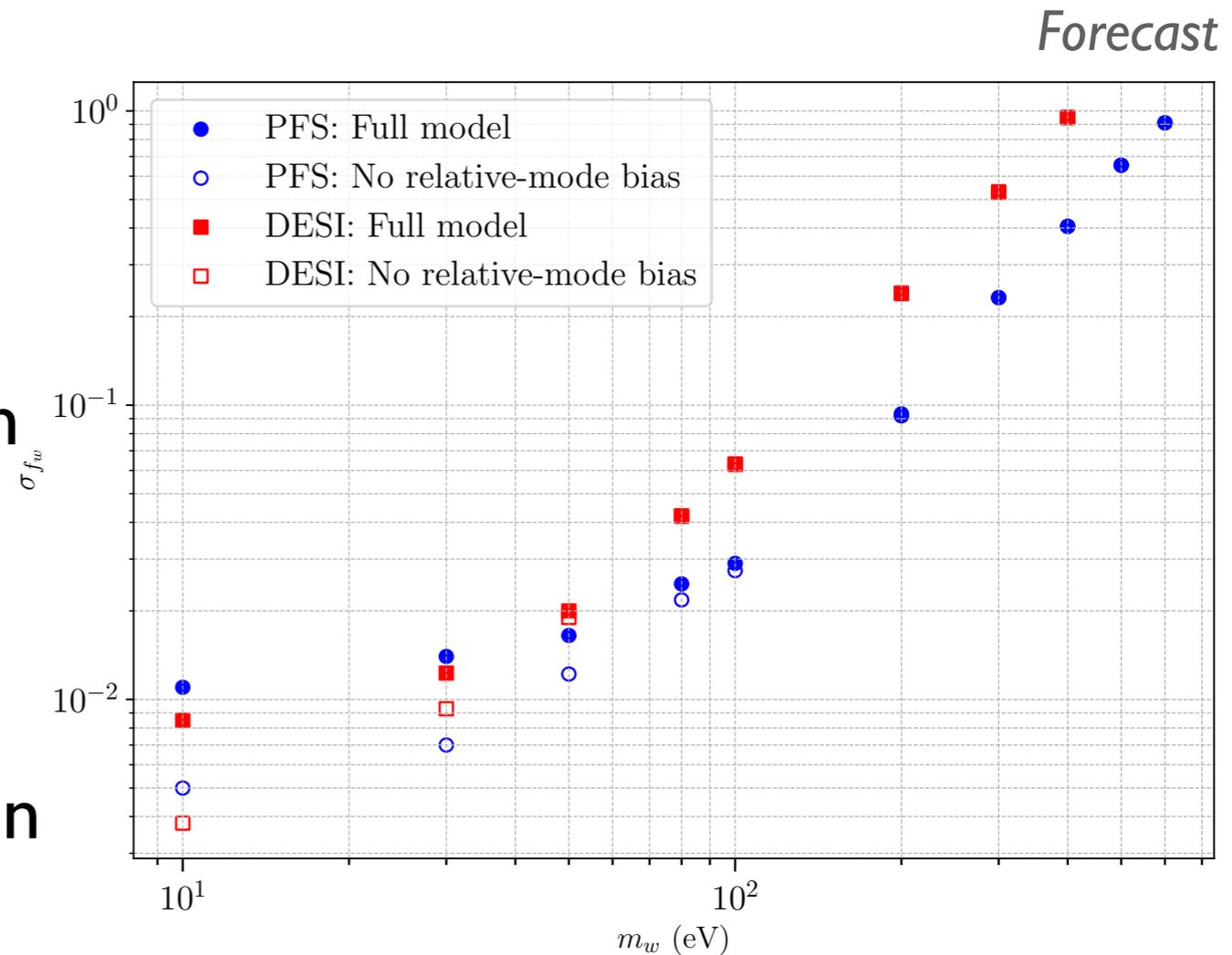
# Dark matter and relics

- Light relic searches are well motivated (*Germino, Lattanzi*) — these could also have finite mass
- Smooth transition to warm DM, but *allow for CDM component*
- Current constraints on non-CDM (WDM, FDM, SIDM) usually assume 100% non-CDM
  - PBH searches on the other hand constrain  $f_{\text{PBH}}$ ...
- Should we allow for CDM component when constraining the temperature and/or interactions of DM? —> *Mixed DM*

# Mixed dark matter



- Interesting effects in LSS — scale-dependent feature at some  $k_{fs}$  with amplitude controlled by  $f_{relic}/WDM$ 
  - Discovery window depending on  $z$  and number density of surveys
- **Relative density & velocity modes** from early universe — need to be taken into account in bias expansion but also have unique signatures
- EFTofLSS and galaxy bias expansion become nontrivial — two complementary approaches pursued



# Summary...

$\omega_c, \omega_b, M_\nu, h, A_s, n_s, (\Omega_\Lambda)$

- ... of my two cents on current constraint analyses:
  - Need to assume some *inflation* prior
  - Neutrino mass constraints are complicated, dataset- and prior-dependent—do not lend themselves to catchy summaries
  - Issues with  $w_0$ - $w_a$  ; use pivot redshift at least, and consider models with more interesting phenomenology
  - Opening up dark matter constraints beyond the 100% single component

